

## David RUELLE

Publications: articles\*

- [1] “Analyticity of Wightman functions at completely space-like points.” *Helv. Phys. Acta* **32**,135-137(1959).
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- [18] “A variational formulation of equilibrium statistical mechanics and the Gibbs phase rule.” *Commun. Math. Phys.* **5**,324-329(1967).
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