

2026: Celebrating FERMI



PROGRAMME

The Enrico Fermi paper "Sulla Quantizzazione del gas perfetto monoatomico" was presented to the Accademia Nazionali dei Lincei by Antonio Garbasso at the Session of February 7, 1926. Franco Rasetti, In the "Collected Papers" by Enrico Fermi, mentions this paper as "probably his most famous theoretical contribution, when he formulated the theory ...of particles...now designated in his honour as fermions"

Thursday 5 February

10.00 *Welcome address*

Carlo DOGLIONI (Presidente della Classe di Scienze Fisiche, Matematiche e Naturali dell'Accademia Nazionale dei Lincei)

Angela BRACCO (Presidente della Società Italiana di Fisica e del Centro Enrico Fermi)

Chair: Massimo INGUSCIO (Linceo, UCBM-Roma, LENS-Firenze)

10.20 Klaus von KLITZING (Max Planck Institute for Solid State Research): *A Century of Fermi Energy: Quantum Hall Physics and Metrology*

11.00 Leonardo FALLANI (Università di Firenze): *New quantum simulations with ultracold Yb fermions*

11.40 Coffee break

2026: Celebrating FERMI



Alessandro Volta: building the future with science

International Conference
Villa Erba, Cernobbio, 14-15 April 2025

Opening event of the celebrations for the bicentenary of the death of Alessandro Volta

From scientific discoveries and research to new technologies and innovation for the benefit of human kind

Program

April 14, 2025 (International World Quantum Day)

15:00 Institutional greetings and introduction

*Chair **Massimo Inguscio**, Accademia Nazionale dei Lincei*

15:30 **Klaus von Klitzing**, *Nobel Prize in Physics 1985, Max Planck Institute*
Electrical Measurements and Quantum Physics

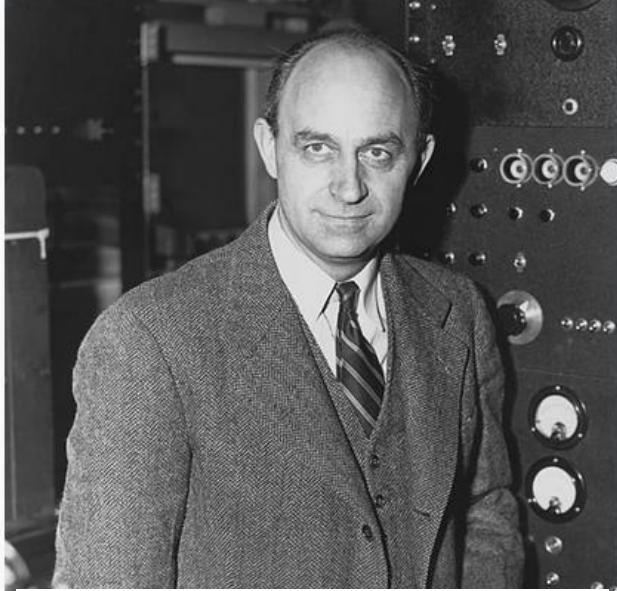
2026: Celebrating FERMI



125th birthday

1901: the year of
the first Nobel Prize

Enrico Fermi
ForMemRS



WIKIPEDIA
The Free Encyclopedia

Fermi in 1943

Born	29 September 1901 Rome, Italy
Died	28 November 1954 (aged 53) Chicago, Illinois, U.S.

Nobel Prize Physics 1938

FERMIOS
FERMI-DIRAC DISTRIBUTION
FERMI-ENERGY
FERMIOLOGY
Composite FERMIOS
.....

Nobel Lecture, December 12, 1938

Artificial Radioactivity
Produced by Neutron
Bombardment

FERMI
unexpectedly saw **FISSION**

VON KLITZING
unexpectedly saw **QUANTUM HALL EFFECT**

On the Quantization of the Monoatomic Ideal Gas

2026: Celebrating FERMI

"Rend. Lincei" 13: 145-149 (1926)
presented by the Associate A. Garbasso at the meeting on 7 February 1926



On the Quantization of the Monoatomic Ideal

Gas

E. Fermi

Introduction

FERMIONS
FERMI-DIRAC DISTRIBUTION
FERMI-ENERGY
FERMIOLOGY
Composite FERMIONS
.....

A recent experiment [1] has brought a nearly-ideal gas of Fermi-Dirac particles (^{40}K atoms) to the condition of *quantum degeneracy*, in which the symmetry of the many-particle wavefunction has a dominant effect on the equation of state of the gas.

In the above-mentioned experiment, the gas atoms were confined by a magnetic field, whose effect is expressed by the harmonic potential,

$$V(x, y, z) = \frac{M}{2} (w_r^2(x^2 + y^2) + w_z^2 z^2)$$

where x, y, z are Cartesian particle coordinates, M is the particle mass, $\omega_r = 2\pi 137$ Hz, and $\omega_z = 2\pi 19.5$ Hz. This situation is close to that portrayed in the

**QUANTUM
Hall Effect**
*** 5 February 1980**

February 5, 2026: A conference day to celebrate TWO birthdays



100th birthday of Fermi-Dirac statistic

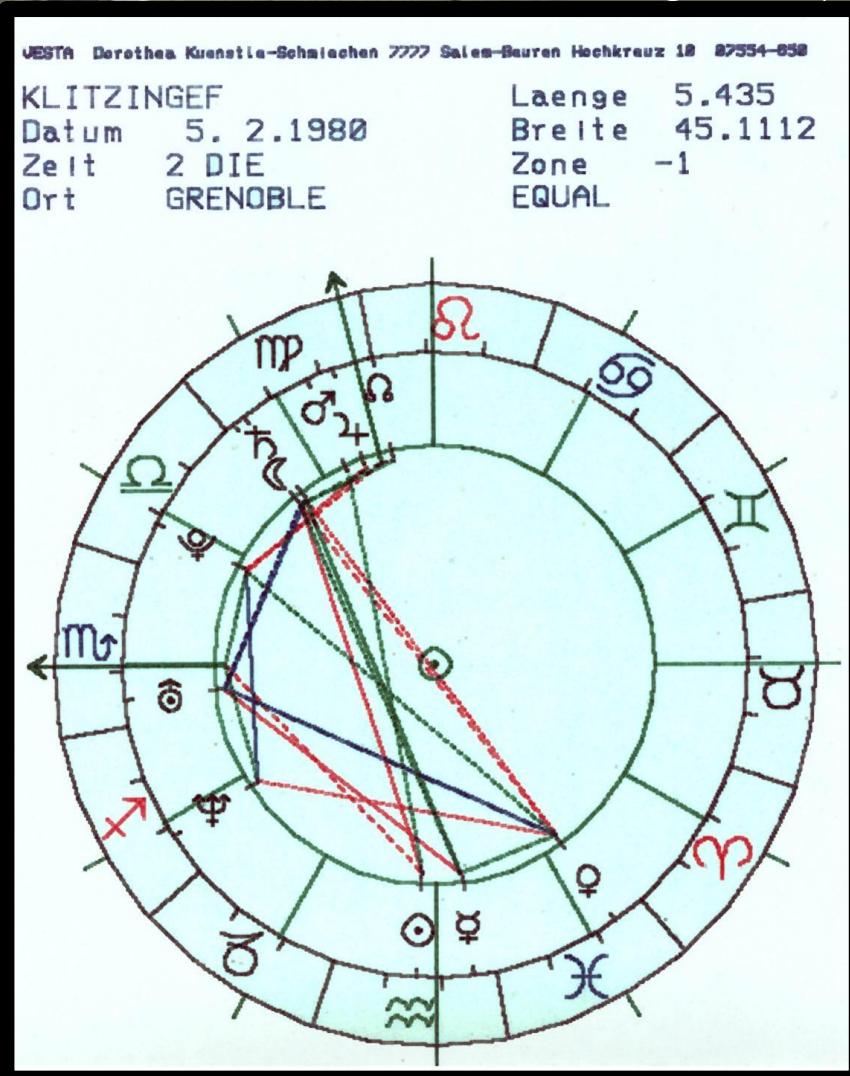
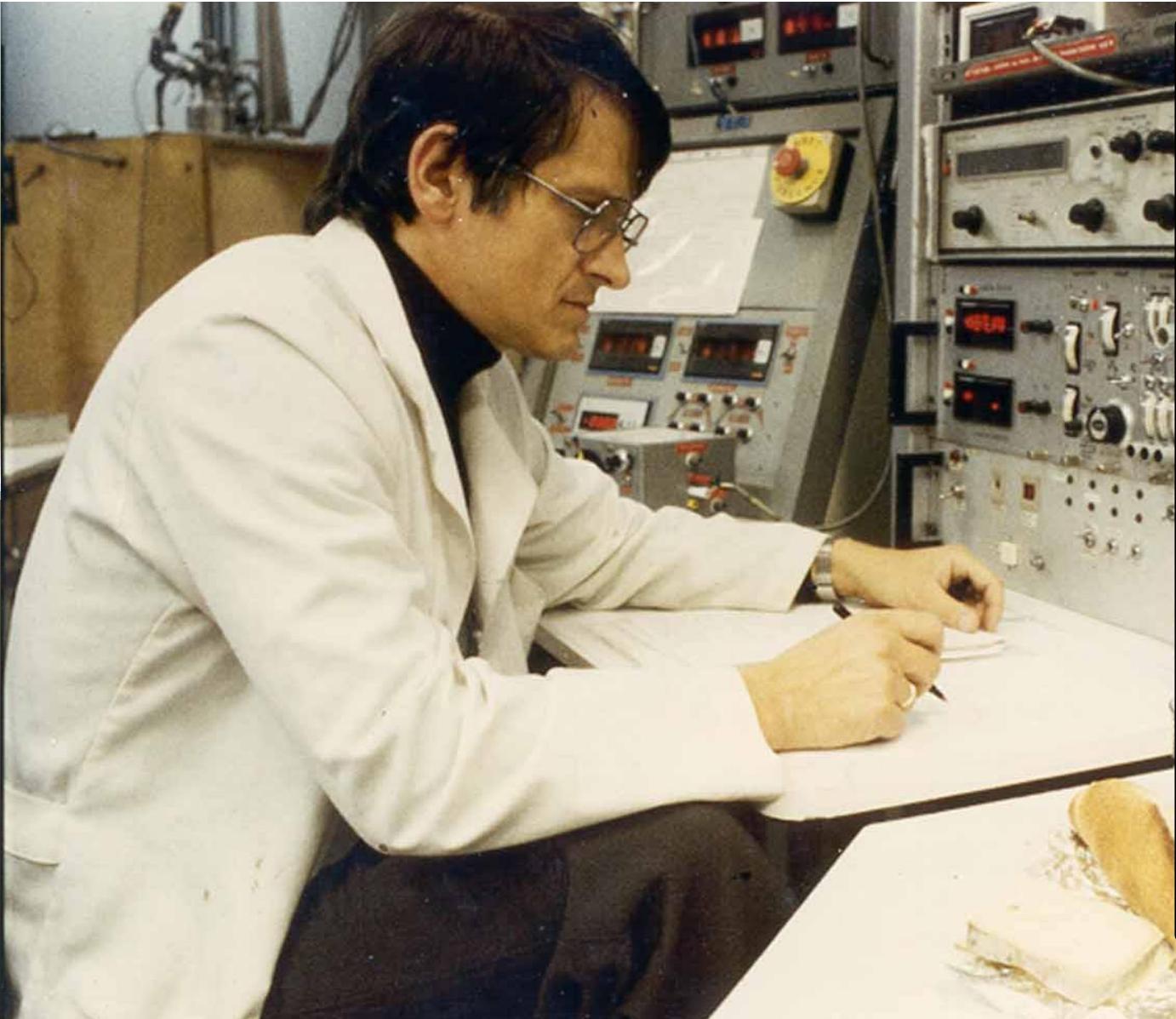


46th birthday of Quantum Hall Effect
with the consequence of a new SI system

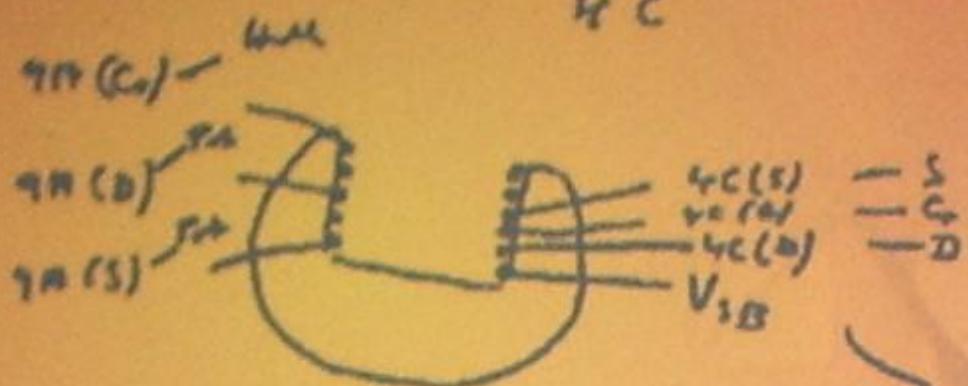
Since 20.5.2019:

New Kilogram
New Ampere
New Kelvin
New Mole

Birth of the Quantum Hall Effect *2/5/1980 at 2 a.m.



Copy of my Notebook



Notizen im Heftaufschluss
vom 4.2.1980



$$U = R \cdot I$$

$$U = \frac{B \cdot I}{e \cdot n \cdot N}$$

$$= \frac{h}{e^2} \cdot I$$

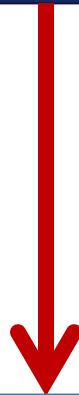
R = Universal Resistance
 $\approx 25812,807.. \text{ Ohm}$

$$R = h/e^2$$

Application of QHE:



A New Electrical Resistor
with a value $R = h/e^2$



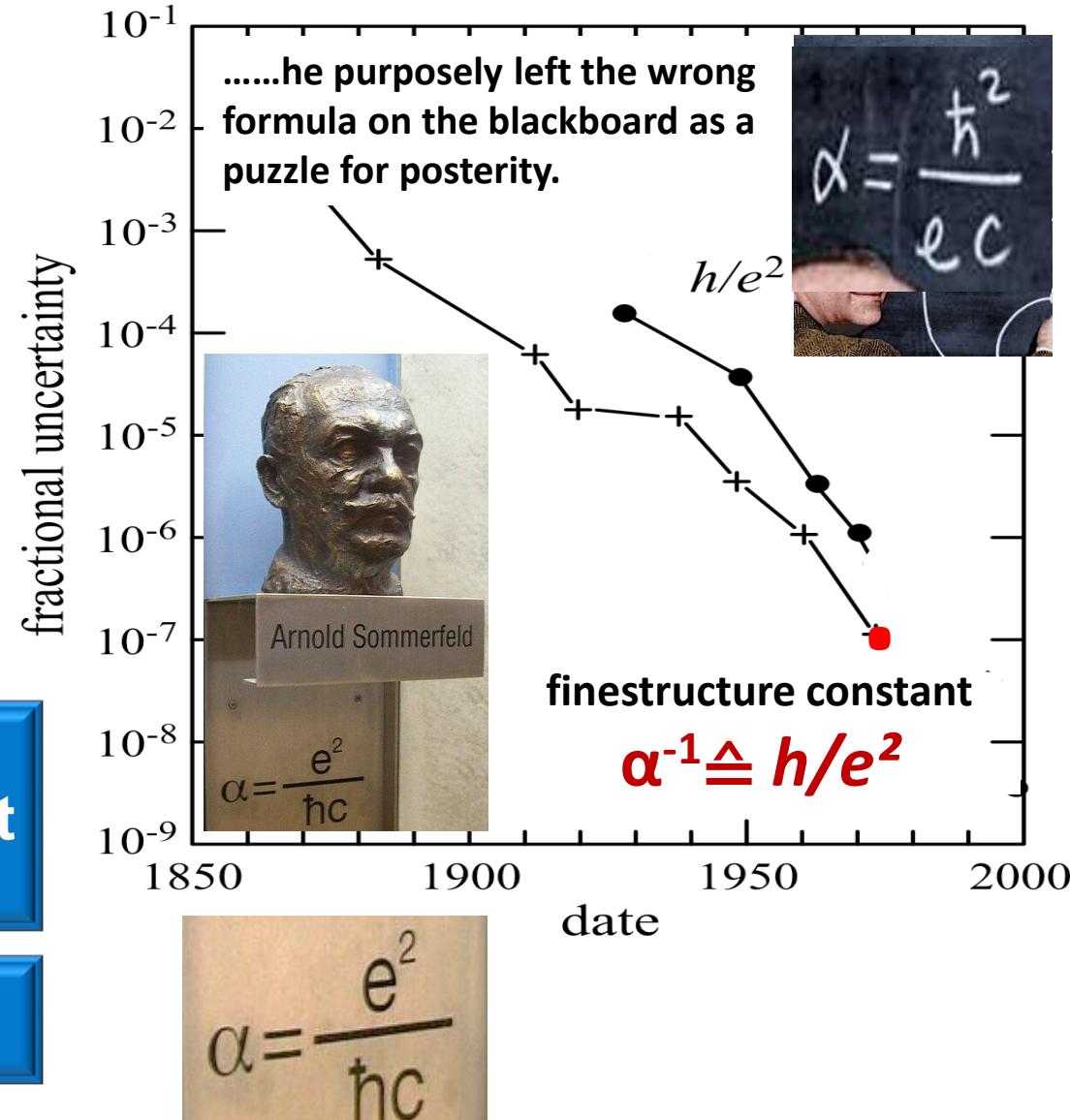
Realization of a
Resistance Standard

If h/e^2 is known

Determination of the
Fundamental Constant

Application 1980

If calibrated Ohm available



Remarks on the quantum theory of the absolute zero of temperature

G. Beck, H. Bethe, and W. Riezler

Die Naturwissenschaften 2, 38-39, (1931)



“Correction”

Die Naturwissenschaften, March 6, 1931

The note by G. Beck, H. Bethe and W. Riezler, published in the January 9 issue of this journal, was not meant to be taken seriously. It was intended to characterize a certain class of papers in theoretical physics of recent years which are purely speculative and based on spurious numerical agreements. In a letter received by the editors from these gentlemen they express regret that the formulation they gave to the idea was suited to produce misunderstanding.

$$T_0 = -(2/\alpha - 1) \text{ degrees.}$$

Putting $T_0 = -273^\circ$ we obtain for $1/\alpha$ the value 137 in perfect agreement within the limits of accuracy with the value obtained by totally independent methods. It can be seen very easily that our result is independent of the particular crystal lattice chosen.

G. Beck, H. Bethe, W. Riezler
Cambridge, 10 December 1930

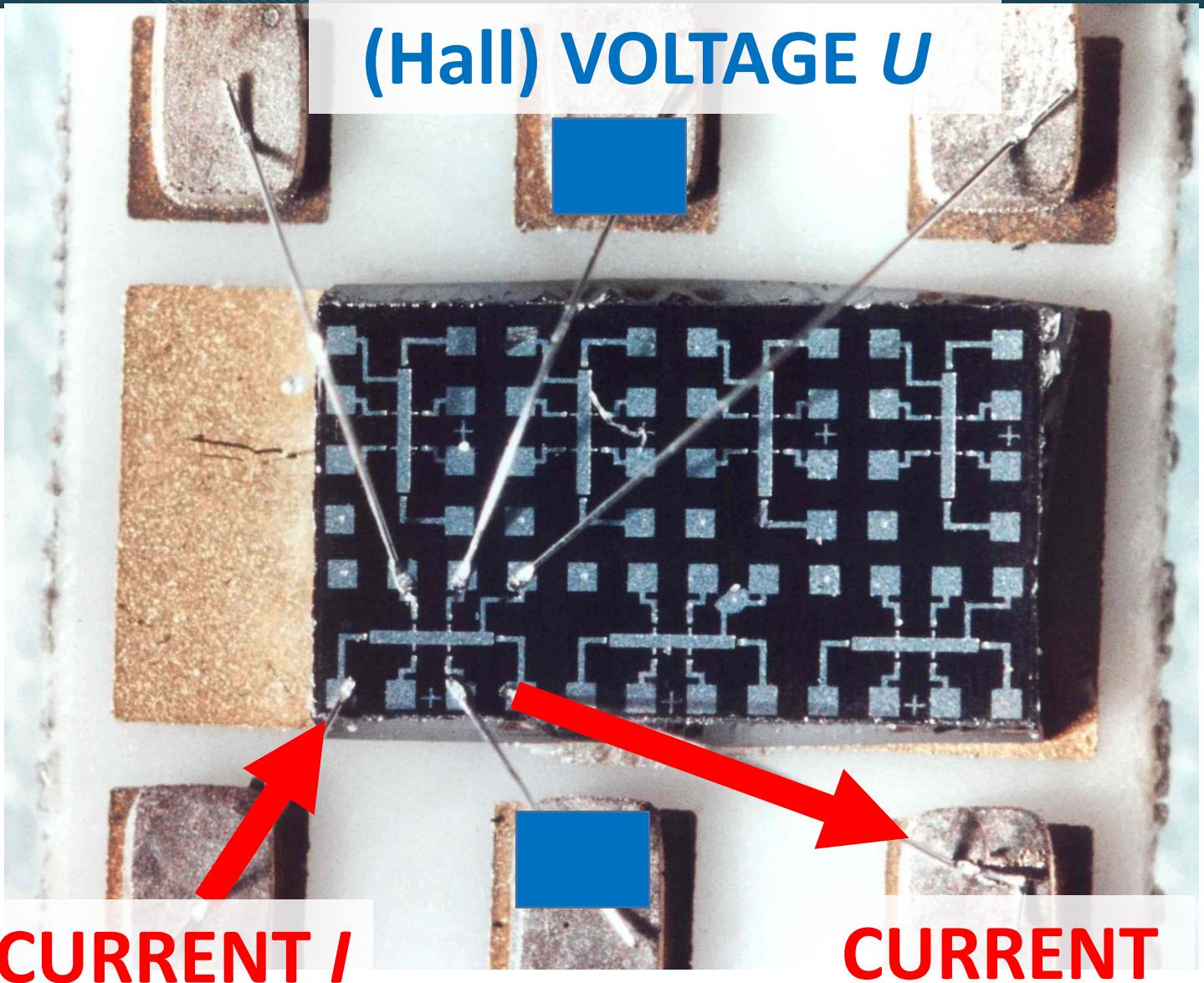
Nobel Prize for
RAMAN

Discovery of the Quantum Hall Effect



My field of research:
How to understand the movement of
electrons in MOSFETs
for smaller and faster devices

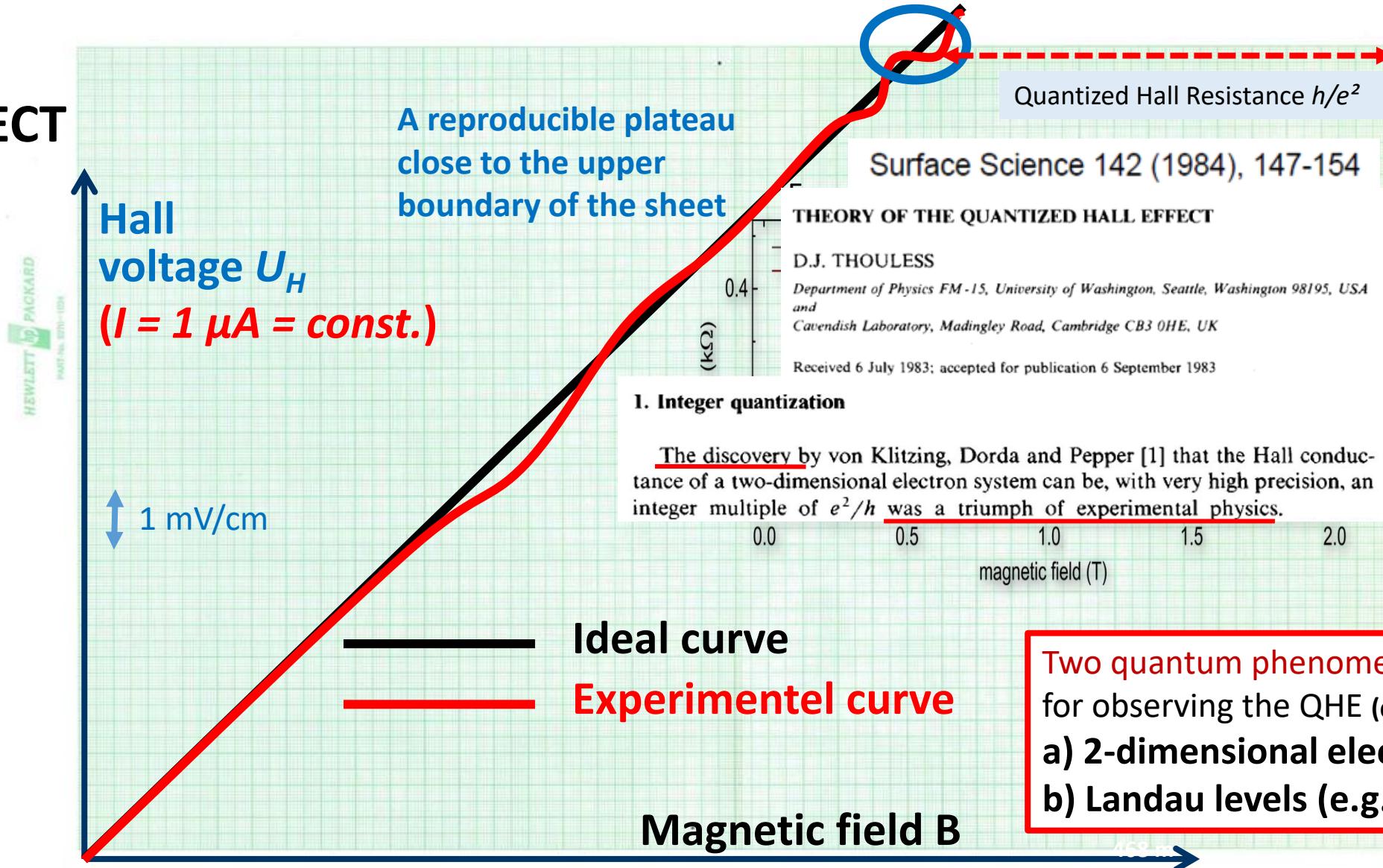
Basic research on the most
important device in
microelectronics (silicon field
effect transistor = MOSFET)
led to the unexpected
discovery of the quantized
Hall effect



From the work of an experimental physicist....



HALL EFFECT



GRAPHENE (atomic layer of Carbon)

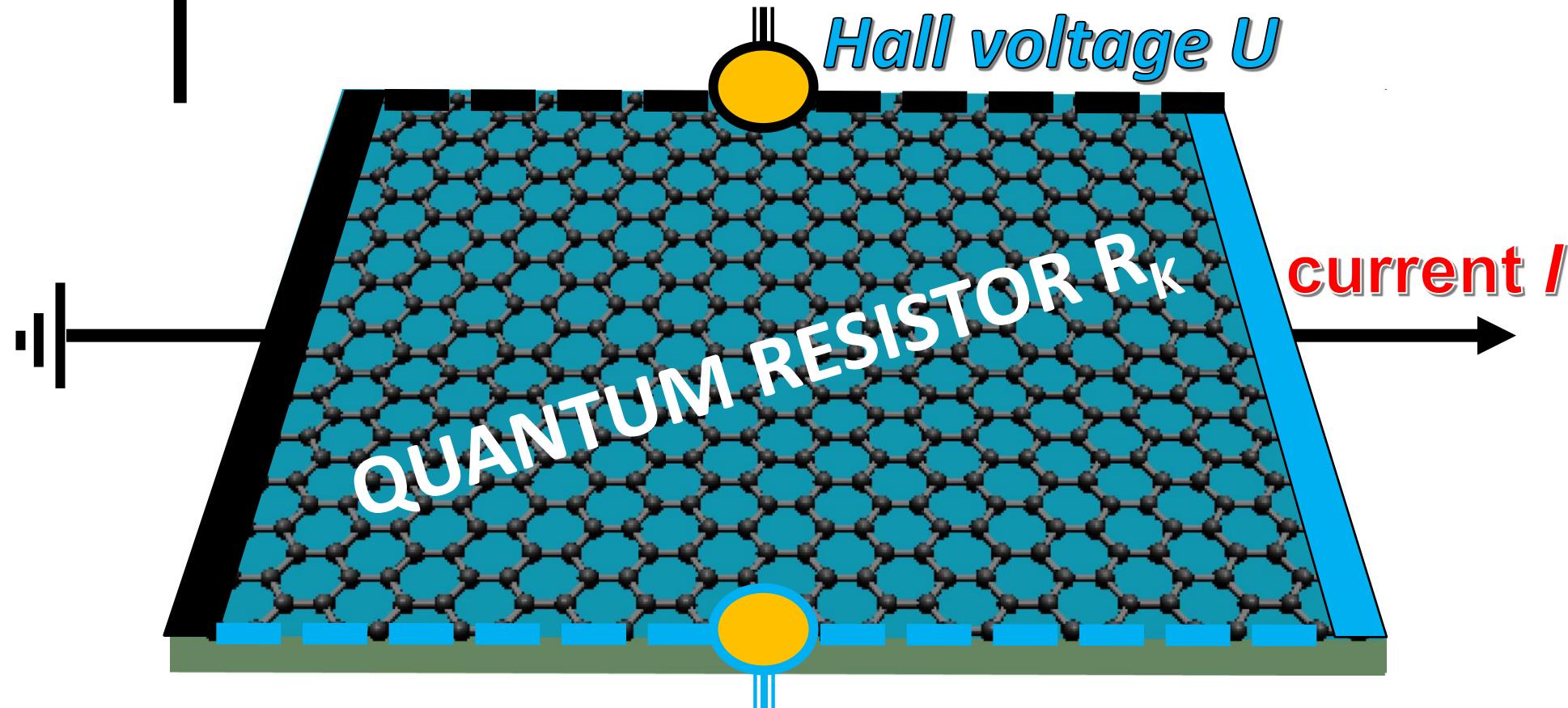
(ideal 2-dimensional conductor):



strong magnetic field

QUANTUM HALL EFFECT

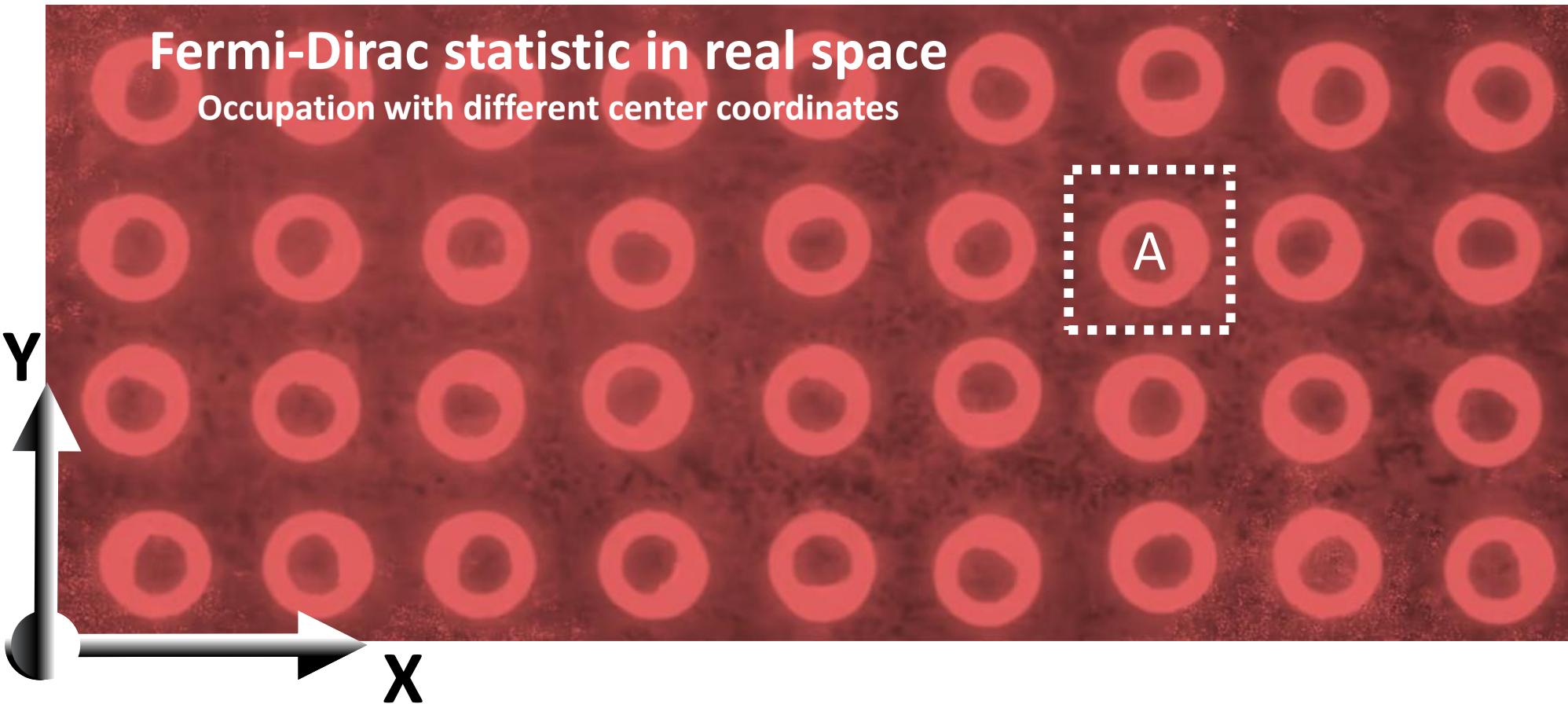
$$\text{Resistance } U/I = h/e^2 = R_K$$



2-dim. electron system + strong magnetic fields:



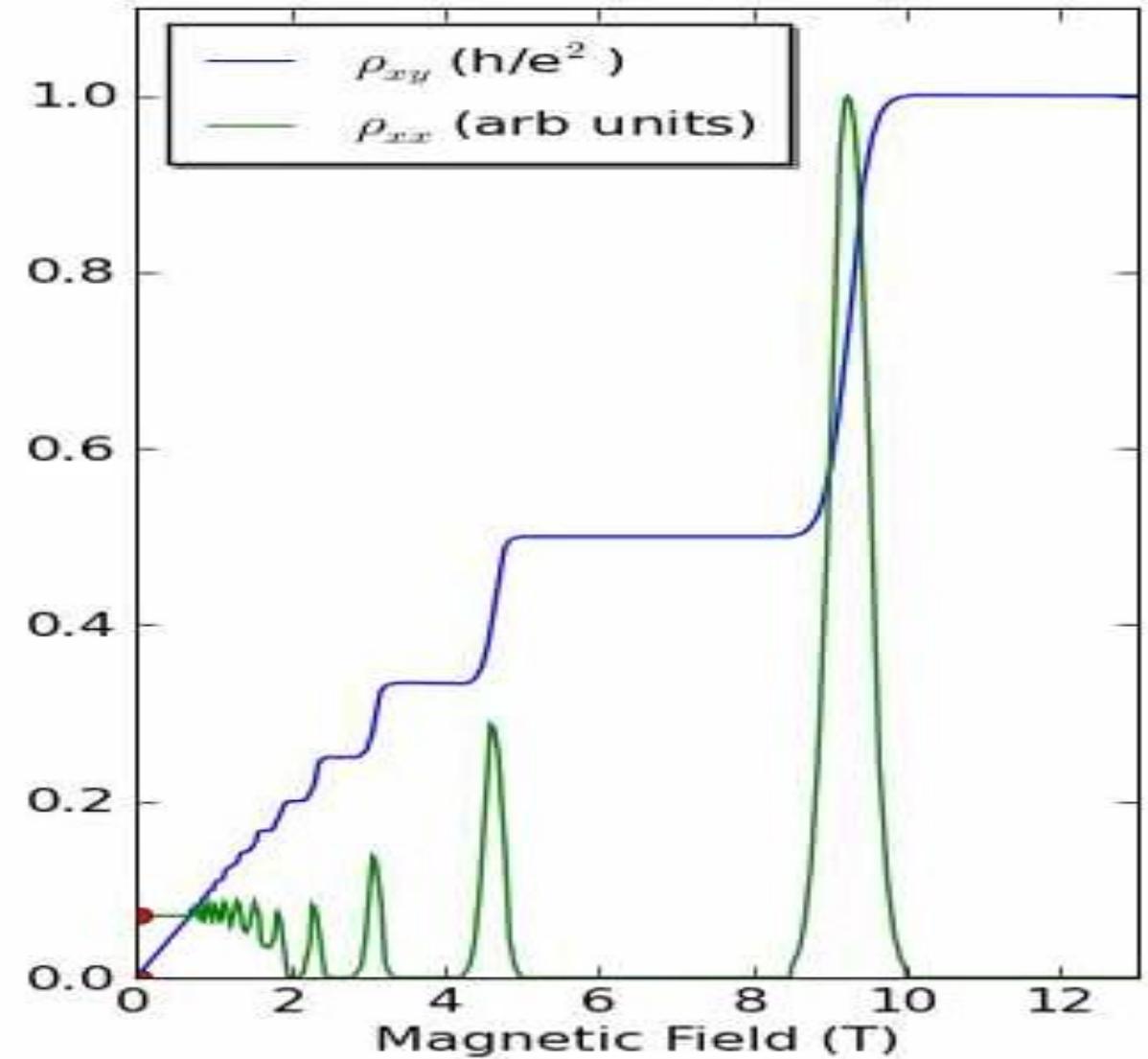
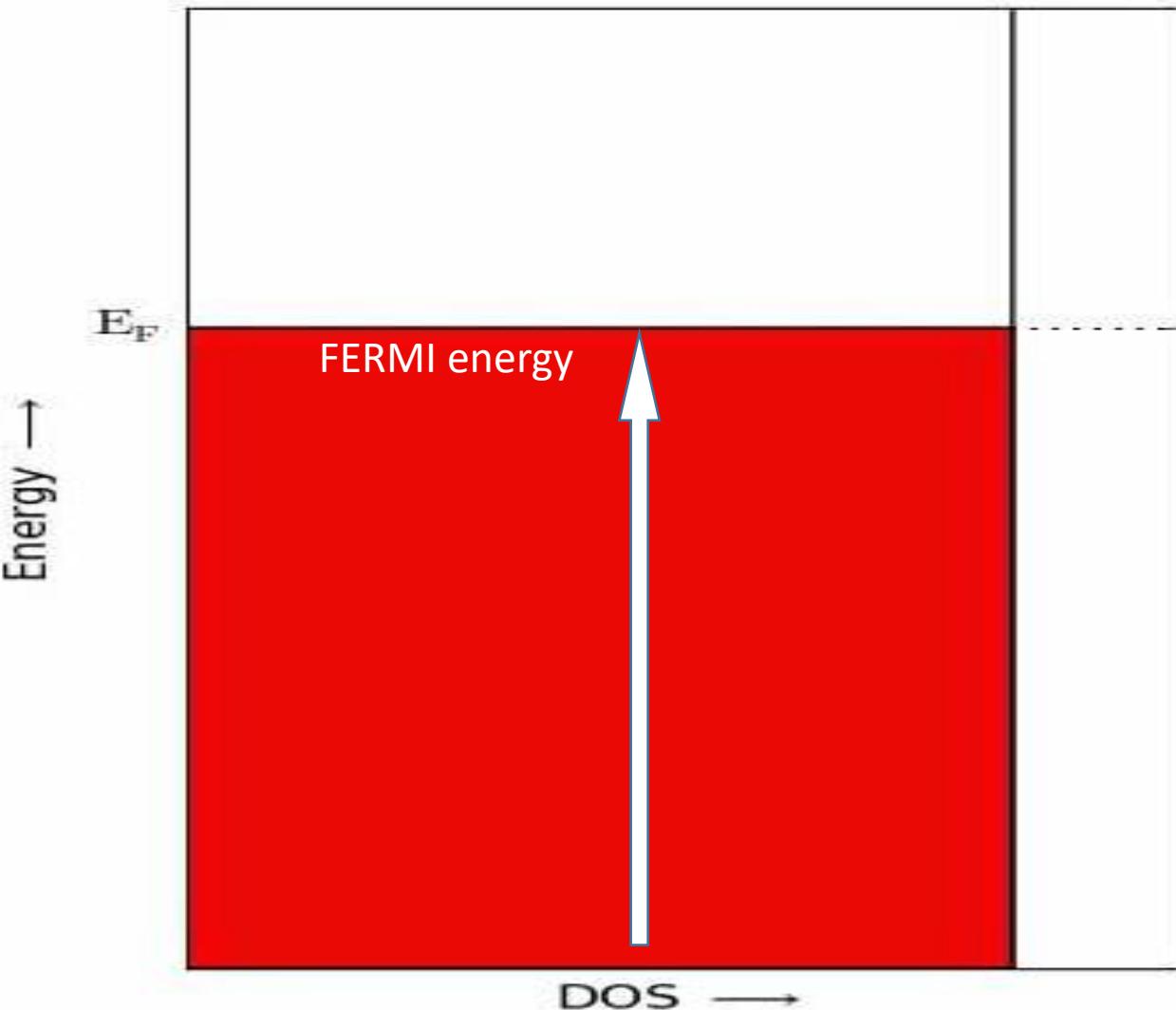
Electrons move on closed cyclotron orbits (like in atomic physics)



Wikipedia Explanation of QUANTUM HALL EFFECT



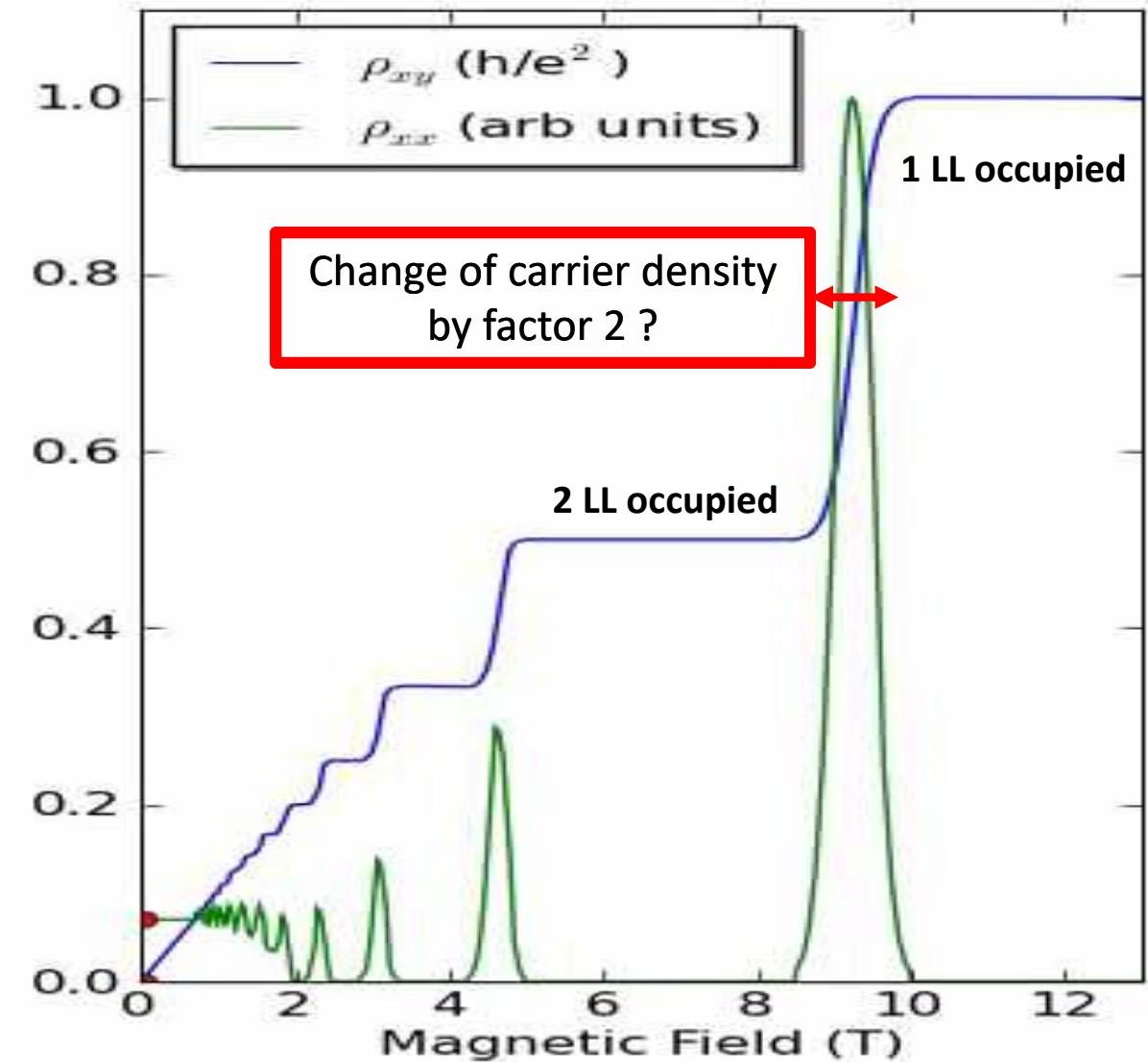
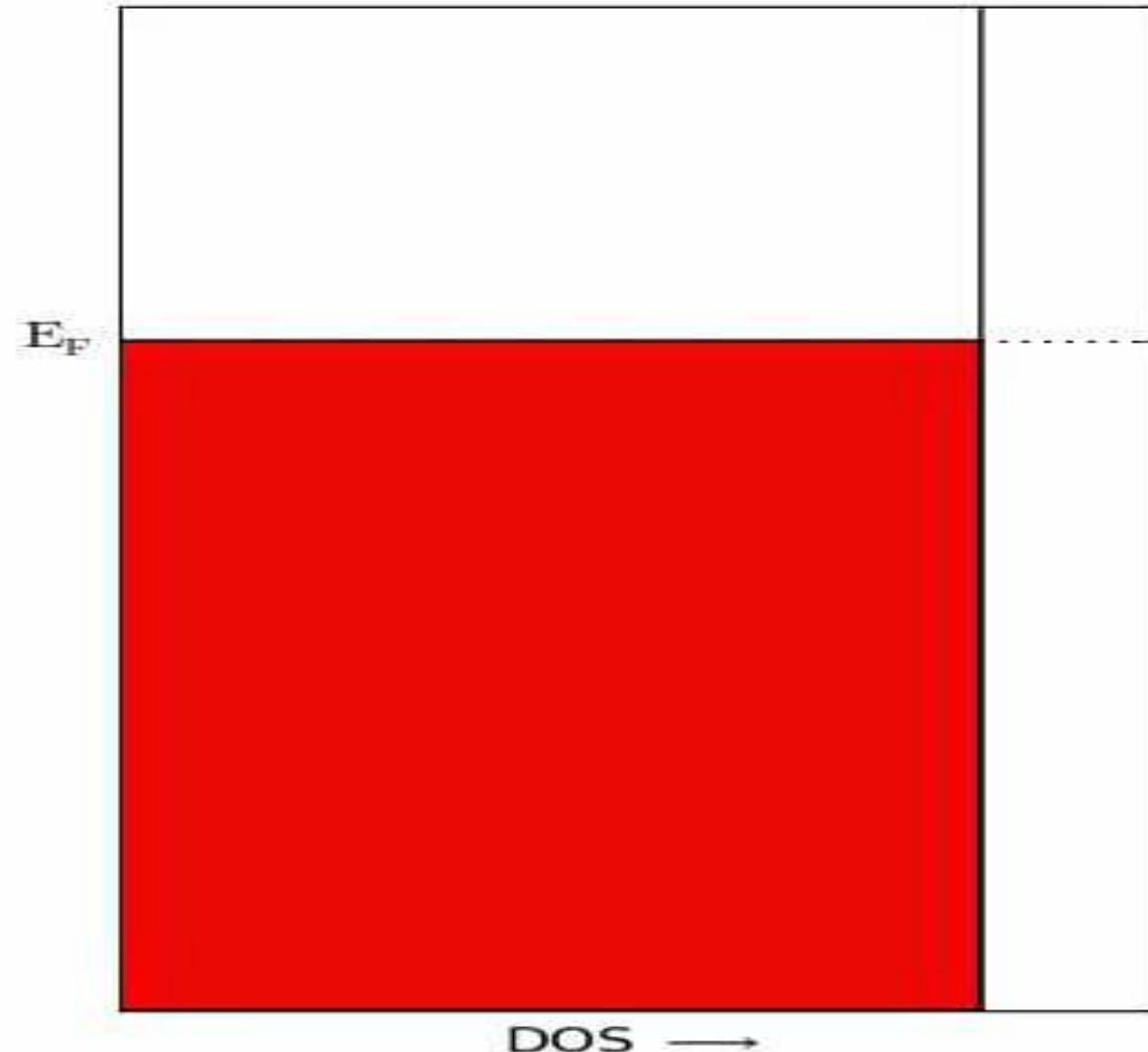
B=0: constant density of states



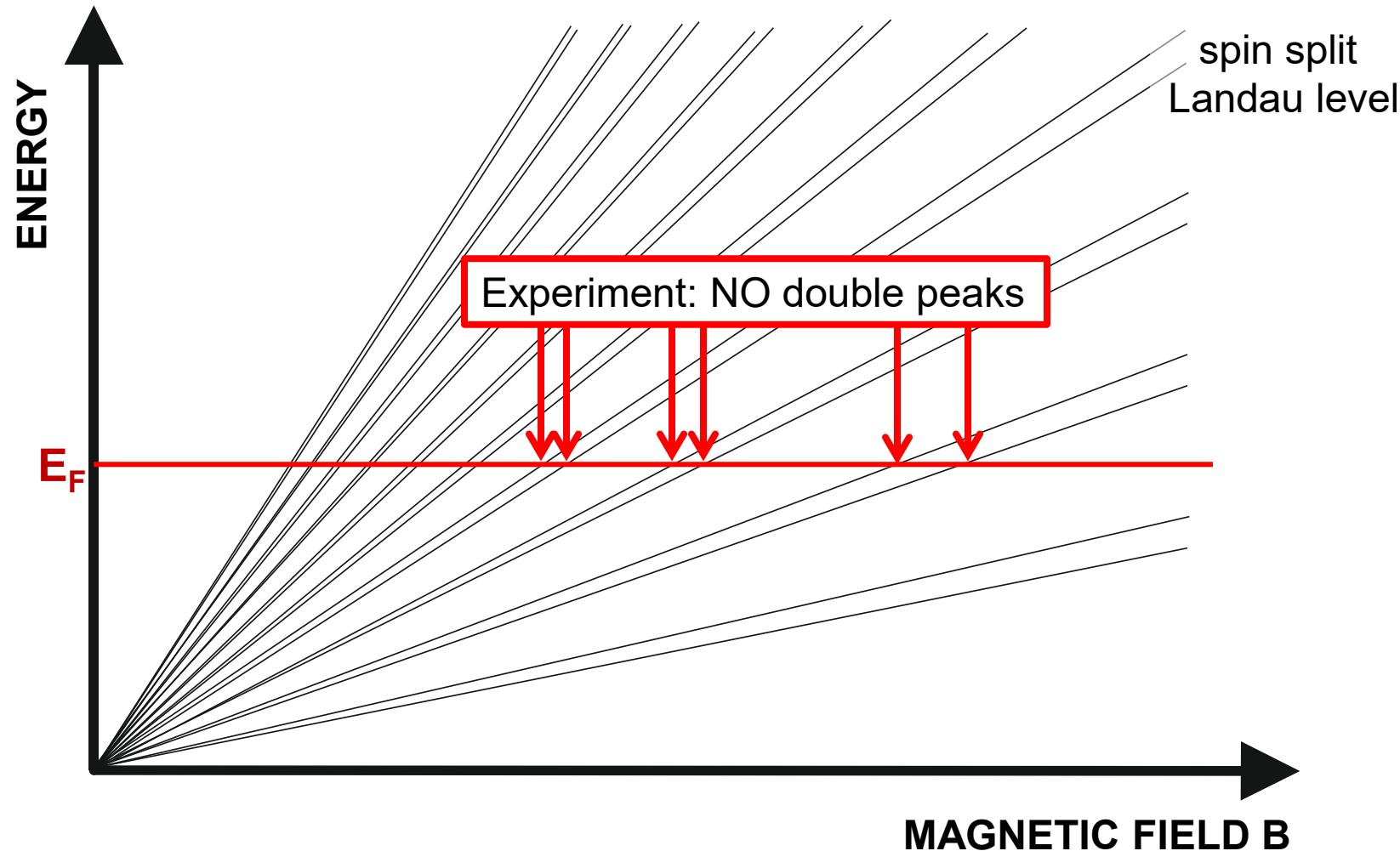
Wikipedia Explanation of QUANTUM HALL EFFECT



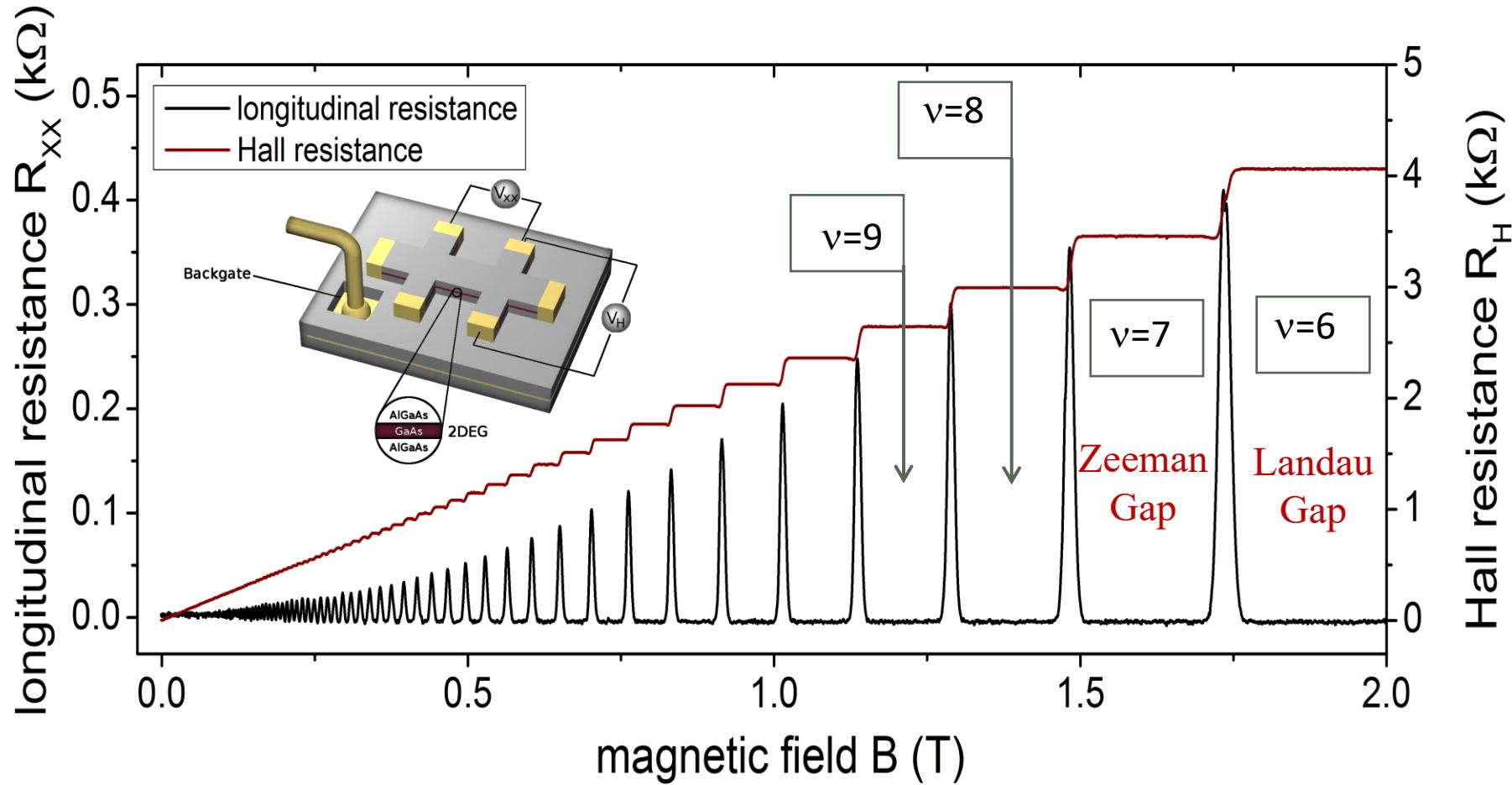
B=0: constant density of states



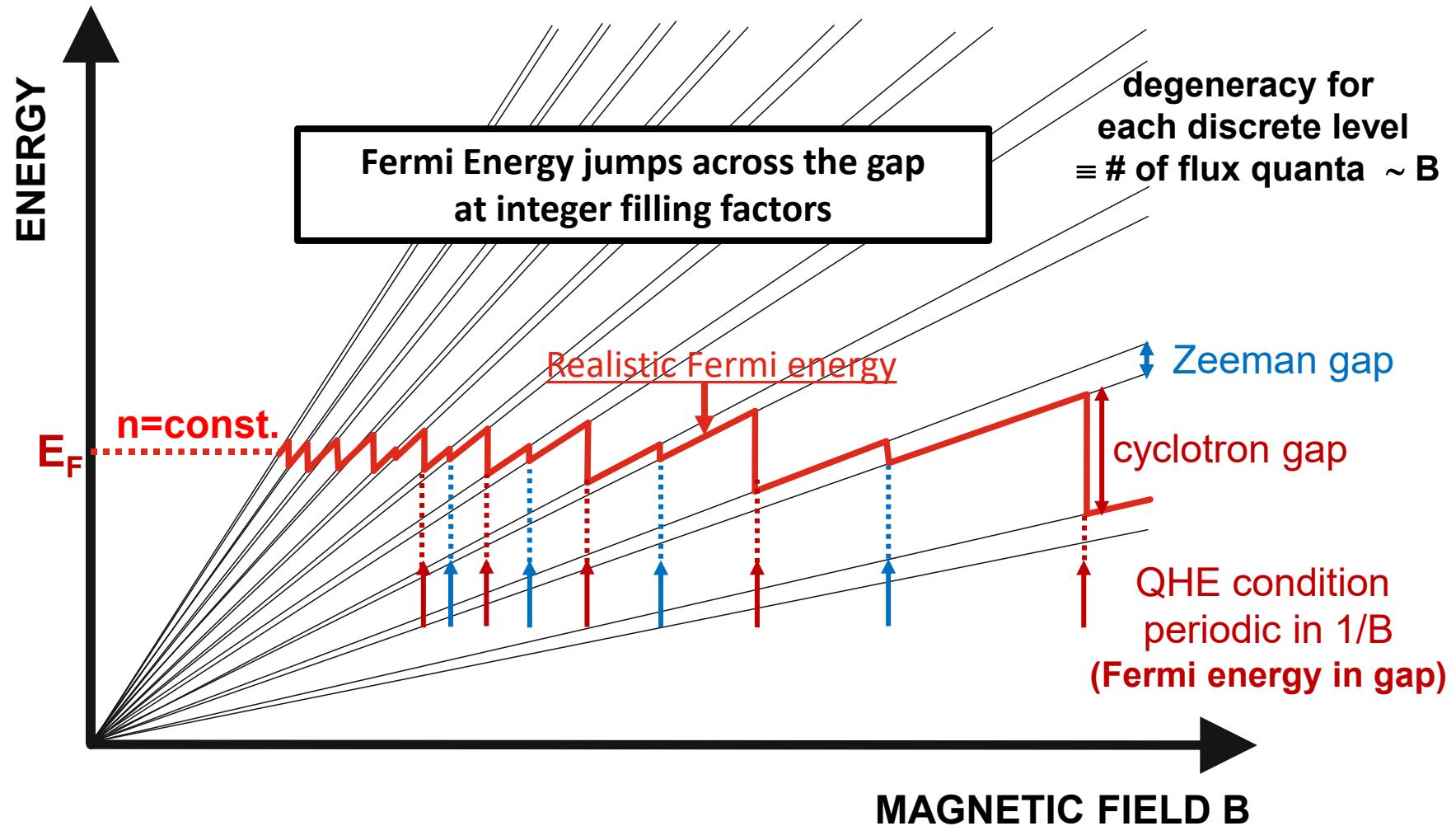
Quantum Hall Devices (GaAs): Spin Splitting of Landau Levels



Integer Quantum Hall Effect for High Mobility GaAs/AlGaAs Heterostructure



Quantum Hall Devices (GaAs): A System with Many Energy Gaps



Jump in Fermi Energy Observable?



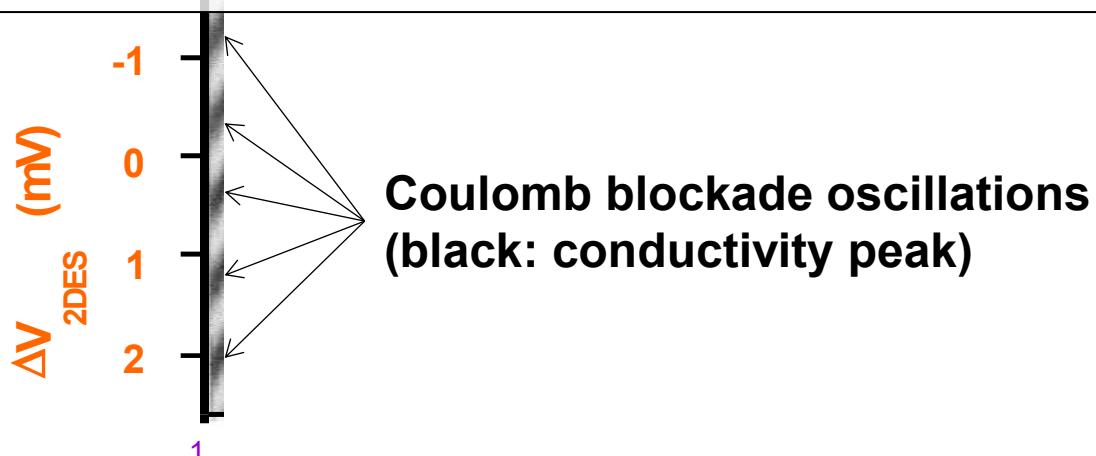
Single Electron Transistor
(SET)

as an extremely sensitive
electrometer for measurements
on a 2DEG

Experiments confirm that
the Fermi energy jumps
at integer filling factor
(energy gap!)

..for the
100th anniversary

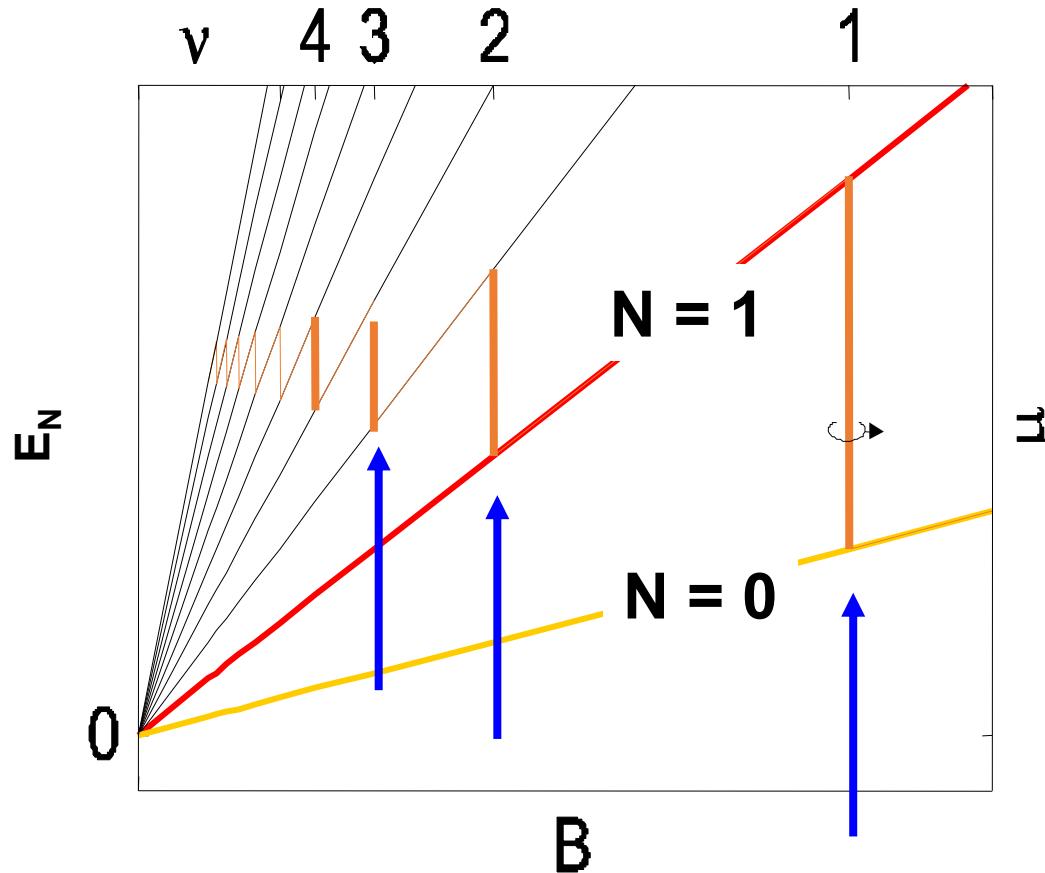
(=gate for SET)





PROBLEMS with „jumping“ Fermi energy

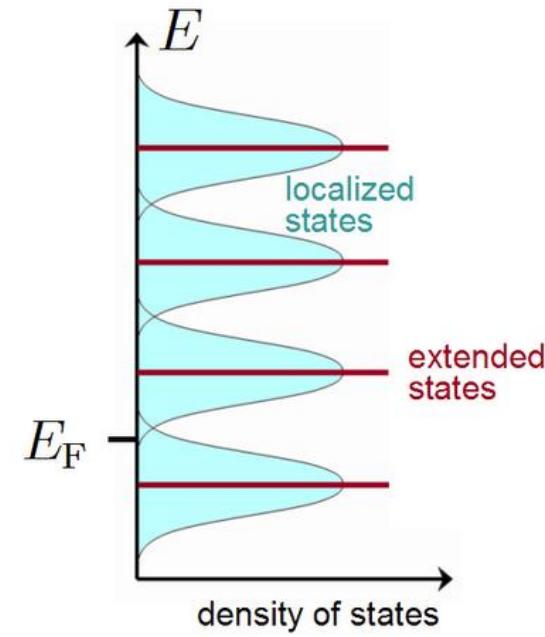
NO quantum Hall **plateaus** since the condition of **fully occupied** Landau level is fulfilled **only for very special magnetic field values!**





A remark must be made on the Hall conductivity σ_{xy} . Even if the Fermi level lies in the Anderson-localized region in the tails of Landau levels there exist the extended states in the sub-band E_F . Since the correlation function of the coordinates (ξ_+, ξ_-) of the electron pair contributes to the Hall conductivity as the correlation function of $\langle \xi_+(t) \xi_-(0) \rangle$, the states below E_F give rise to the Hall conductivity $-\frac{nec}{h}$, where n is the number of mobile carriers below E_F . This is consistent with the experimental

Localized states in the tails of Landau levels are missing in the Hall effect !?



Experimental Facts: The quantized Hall resistance is extremely reproducible !



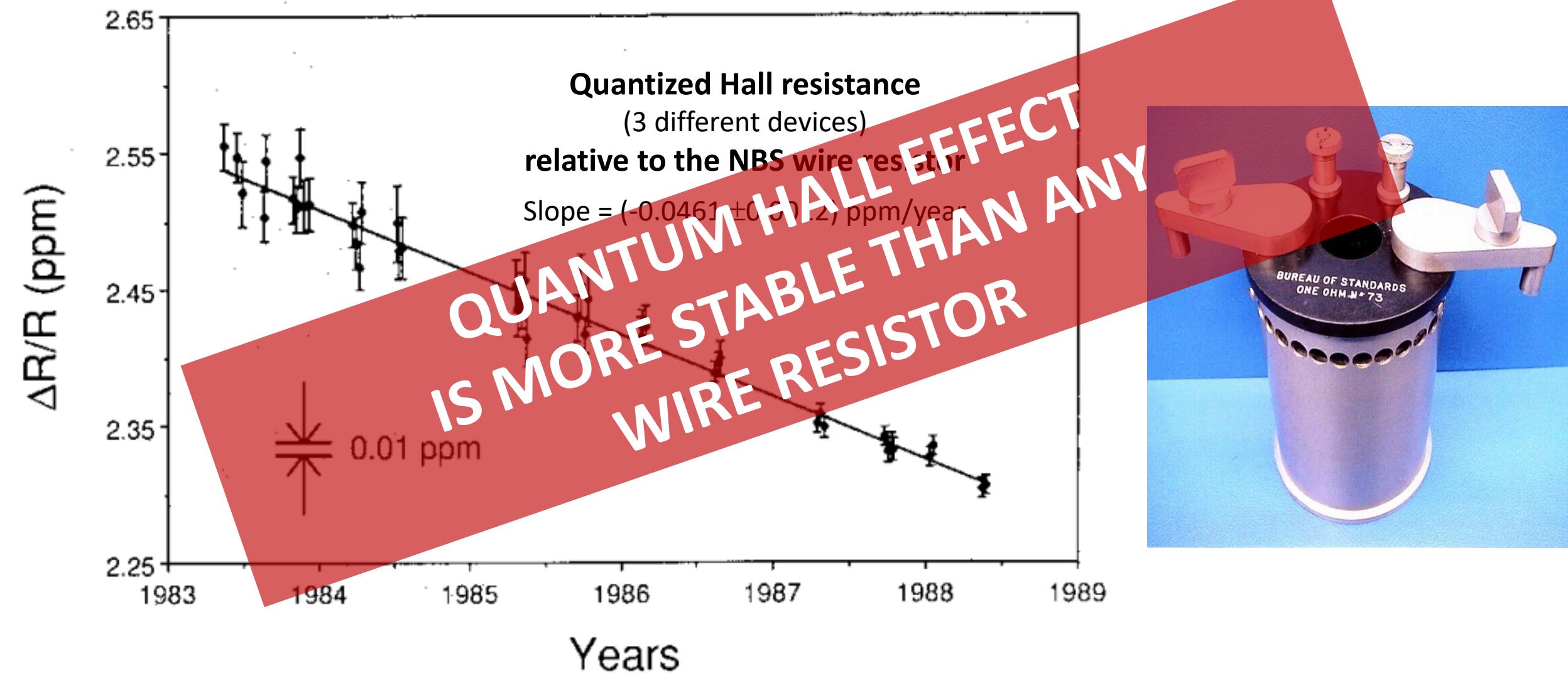
von Klitzing, K. et al. (1980)	25812.68 (8) Ω
BIPM (France)	25812.809 (2) Ω
PTB (Germany)	25812.802 (3) Ω
NBS (USA)	25812.807 (1) Ω
LCIE (France)	25812.802 (6) Ω
NRC (Canada)	25812.814 (6) Ω
NPL (UK)	25812.809 (1) Ω
ETL (Japan)	25812.806 (7) Ω
IMS (Russia)	25812.807 (8) Ω
VSL (The Netherlands)	25812.802 (5) Ω
NIM (China)	25812.806 (16) Ω
EAM (Switzerland)	25812.809 (4) Ω

Task Group “Quantum Hall” at NBS

Monitoring the U.S. Legal Unit of Resistance via the Quantum Hall Effect



IEEE TRANSACTIONS ON INSTRUMENTATION AND MEASUREMENT, VOL. IM-36, NO. 2, JUNE 1987

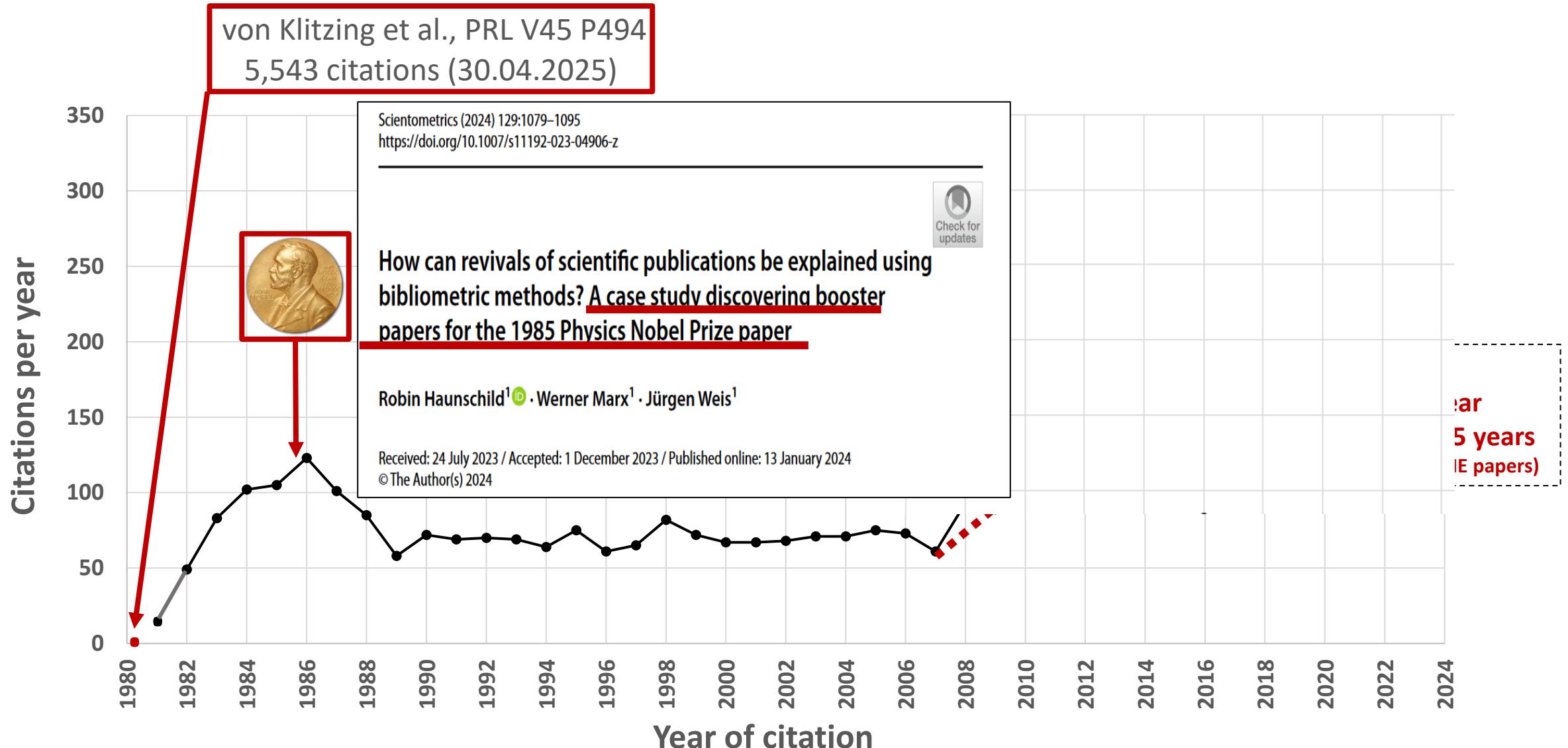




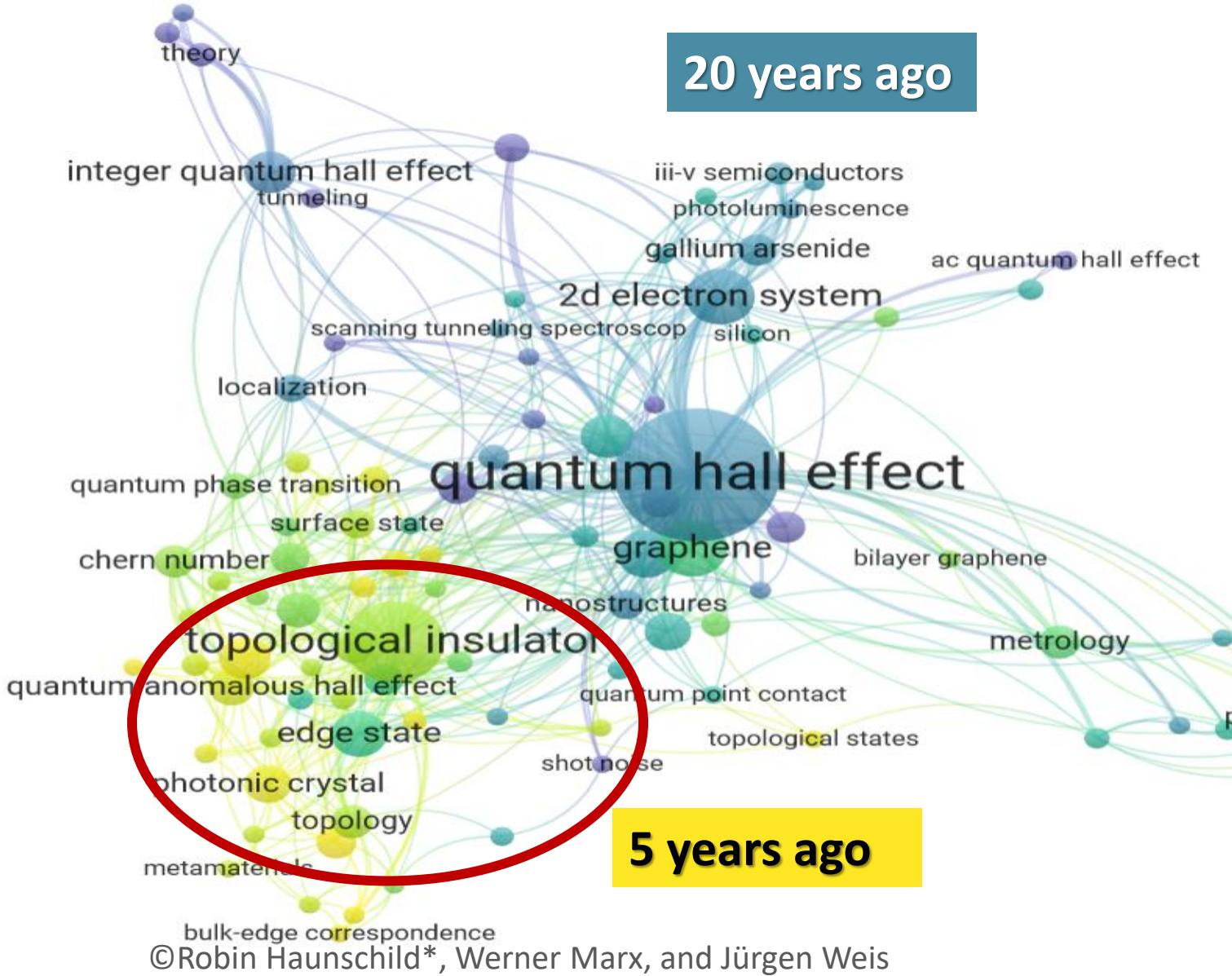
QUANTUM HALL EFFECT

Opened a new research field
(including application in metrology)

First Quantum Hall Publication: 11.8.1980



Impact of the Original QHE Publication



QUANTUM HALL EFFECT: THE FIRST TOPOLOGICAL INSULATOR

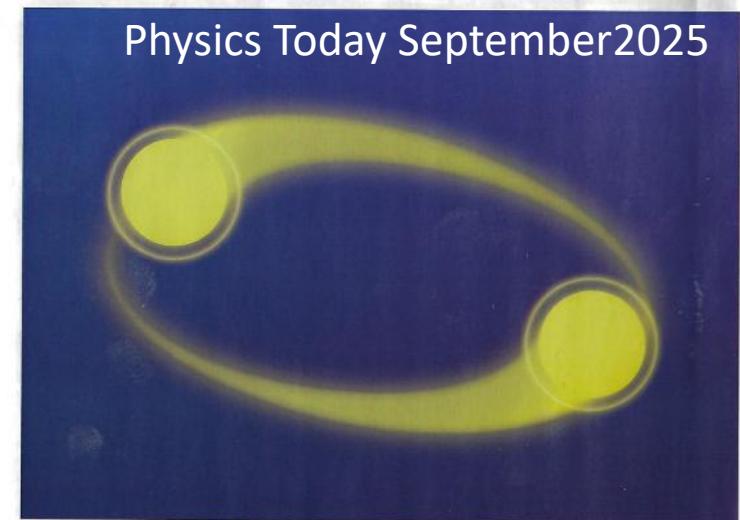


FIGURE 1. WHEN IDENTICAL PARTICLES change places, their quantum statistical character shines through. In three spatial dimensions, exchanging particles twice is the same as leaving them alone, and it follows that particles must be either fermions or bosons. But in reduced-dimensional spaces, there's a spectrum of other possibilities. (Figure by Freddie Pagan.)

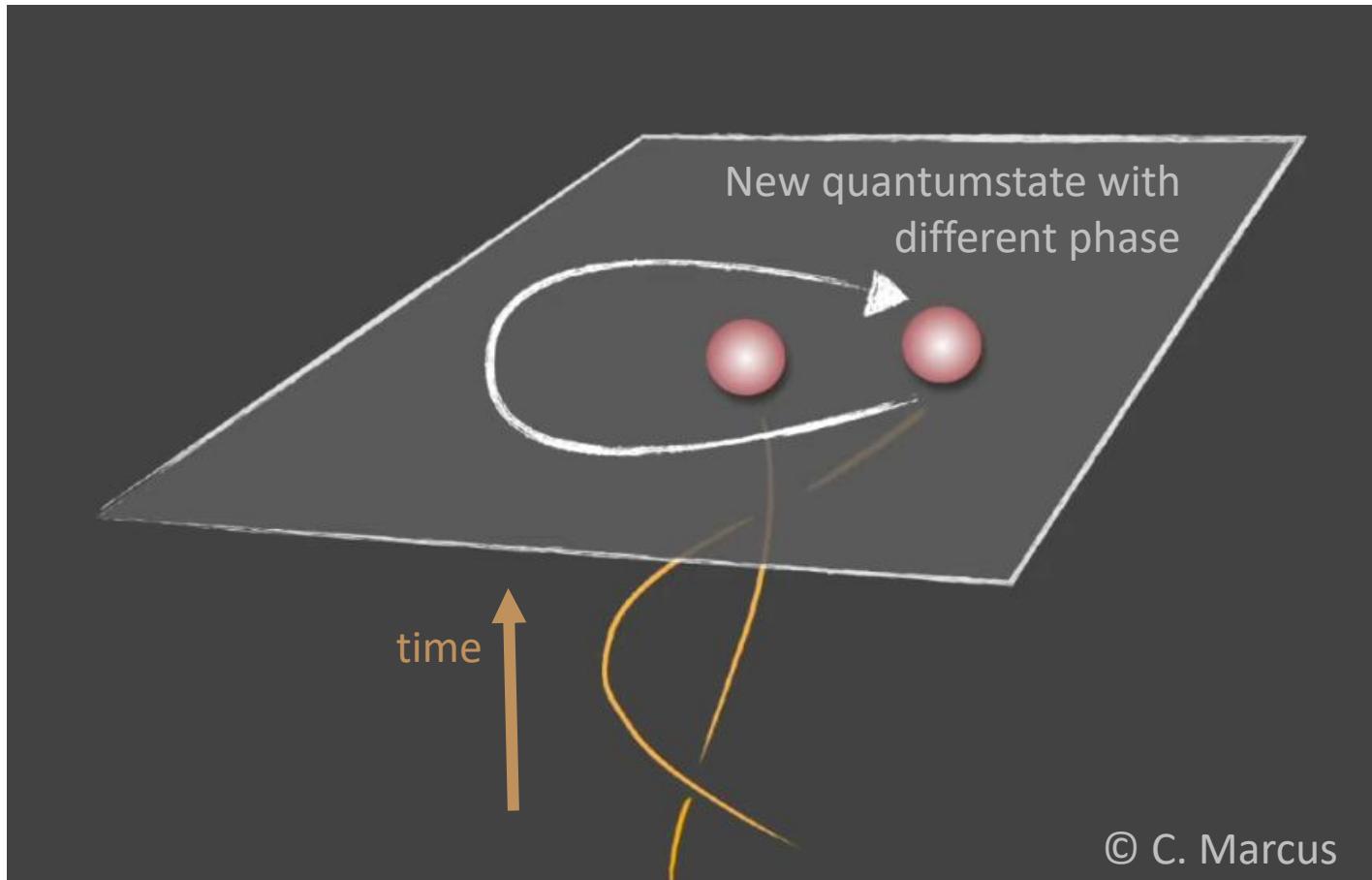
12 PHYSICS TODAY | SEPTEMBER 2025

2006 2008 2010 2012 2014 2016 2018 2020

Speciality of 2-dimensional systems:



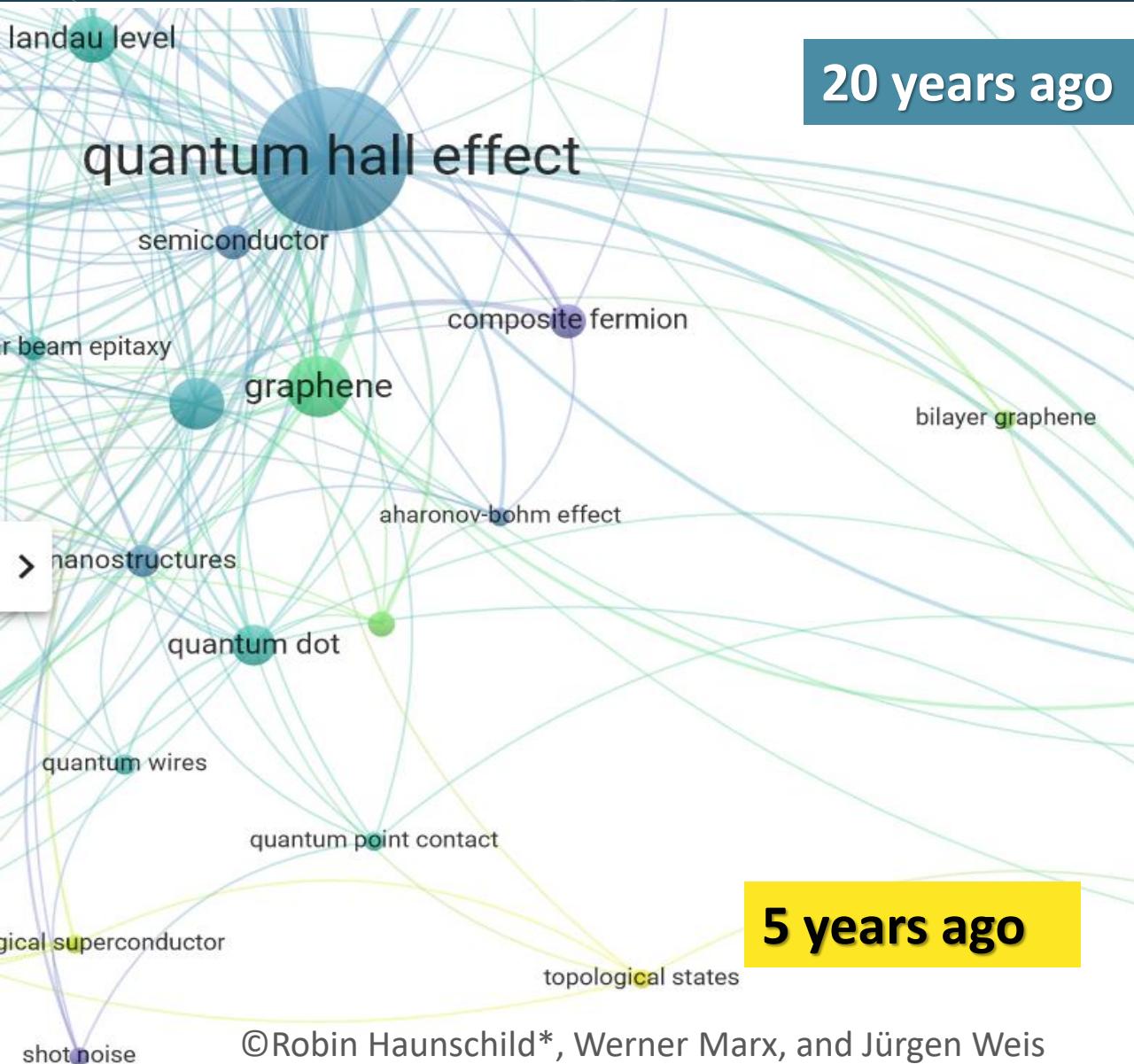
Particles behave not only as **FERMIOS** or BOSONS but also as **ANYONS** (any-ons)



Impact of the Original QHE Publication



Impact of the Original QHE Publication



20 years ago

QHE and Metrology

Quantized Hall resistance revolutionized
(≈ 40 years after the discovery)
our *International System of Units*



5 years ago

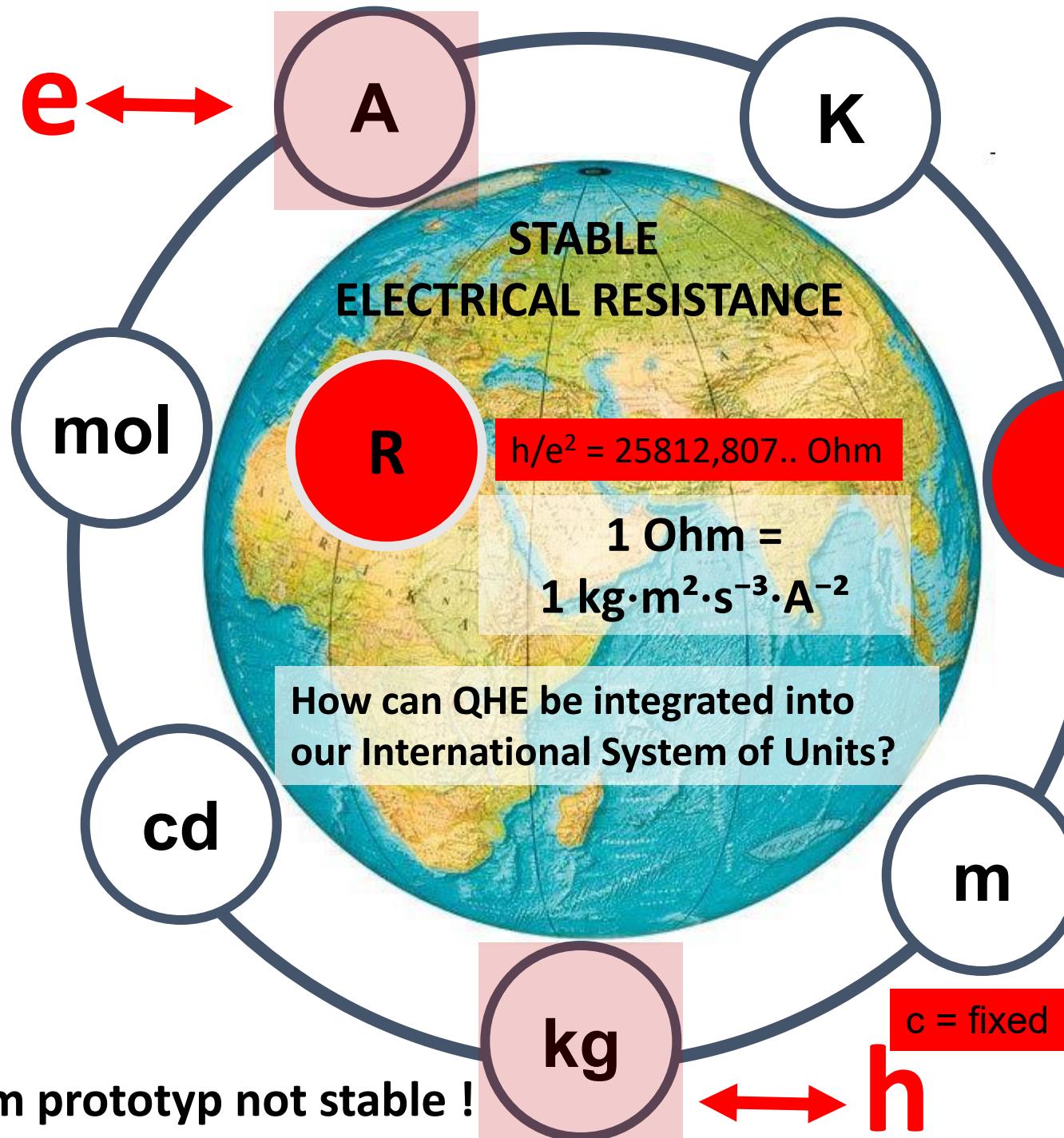
INTERNATIONAL SYSTEM OF UNITS



ALL MEASUREMENTS IN OUR UNIVERSE CAN BE TRACED
BACK TO THE 7 BASE UNITS OF OUR SI SYSTEM:
KILOGRAM, METER, SECOND, AMPERE, KELVIN, MOL, CANDELA



May 20, 2019,
worldwide change in measurement laws



7 SI base units

Situation 10 years ago

**atomic clock
(since 1967)**

$$\hbar/e^2 = 25812,807.. \text{ Ohm}$$

$$1 \text{ Ohm} = 1 \text{ kg}\cdot\text{m}^2\cdot\text{s}^{-3}\cdot\text{A}^{-2}$$

How can QHE be integrated into our International System of Units?

Fixed value for
velocity of light
(since 1983)

Kilogram prototyp not stable !

The metre is defined by taking the fixed numerical value of the speed of light in vacuum, c , to be 299 792 458 when expressed in the unit m/s.

A Historical Event

26th Meeting of the International Committee of Weights and Measure



Representatives of the Meter Convention voted unanimously to redefine four basic units of measurement: the kilogram, the mole, the kelvin, and the ampere. Among them was Klaus von Klitzing, front row, taking a picture, discoverer of the von Klitzing constant in 1980, for which he received a Nobel Prize.

Credit...Matt Roth for The New York Times

Standing Ovation



For a New International System of Units
(fixed values for natural constants)



A Historical Event!



Quantum metrology united all countries

New Definitions of SI Units



KILOGRAM

~~prototype~~

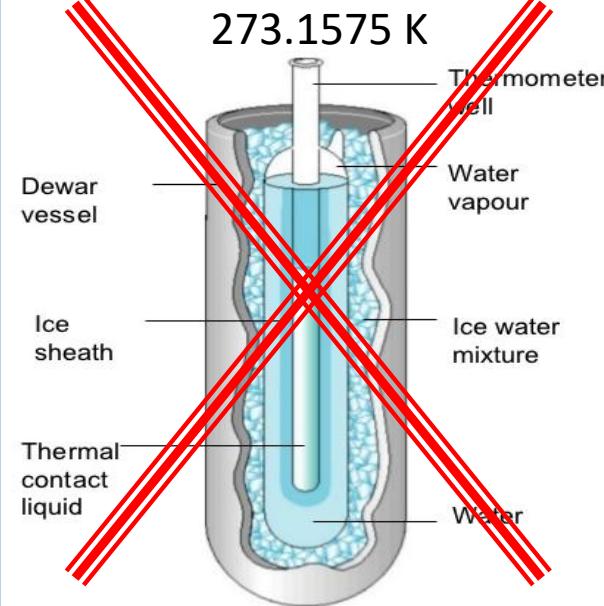


Quantum Kilogram

$$h \equiv 6.626\ 070\ 15 \times 10^{-34} \text{ J s}$$

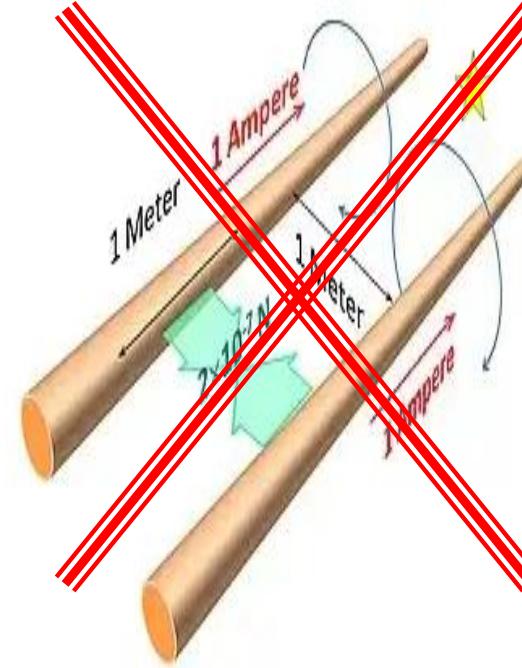
KELVIN

~~triple point cell~~



AMPERE

~~force between 2 wires~~



MOLE

~~# of atoms
in 12 g C¹²~~



$$N_A \equiv 6.022\ 140\ 76 \times 10^{23} \text{ mol}^{-1}$$

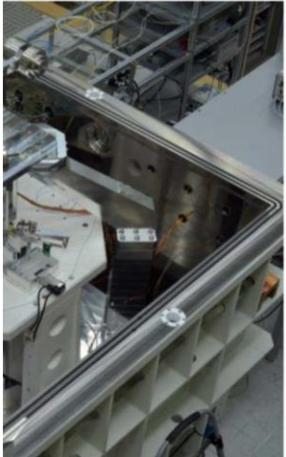
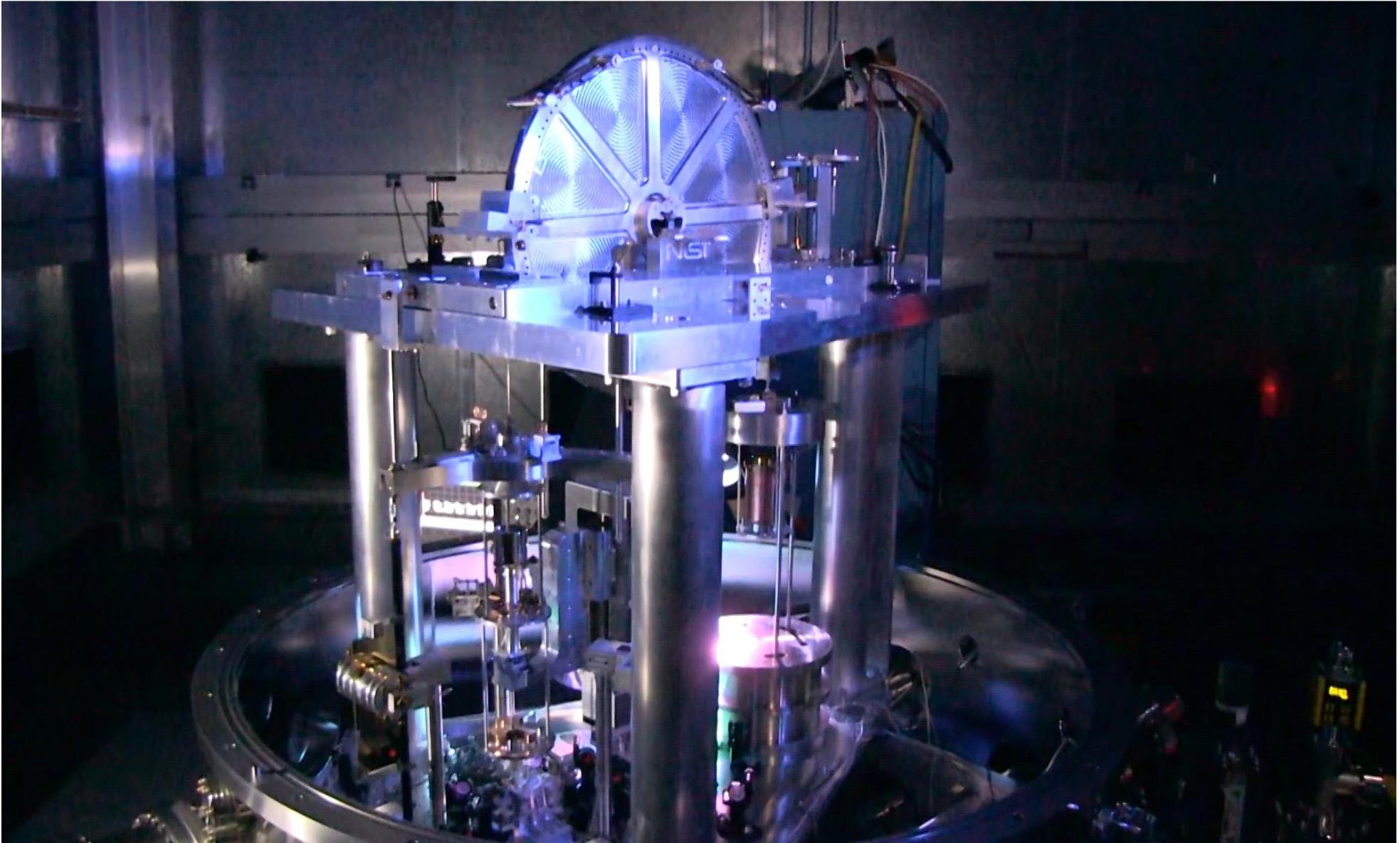
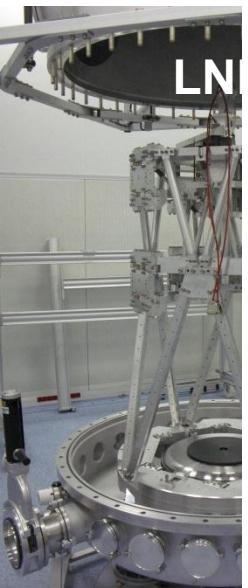
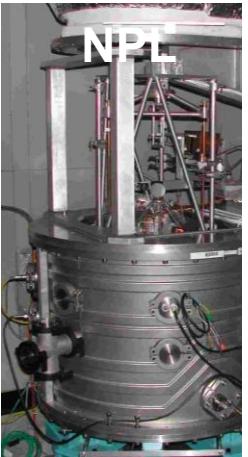
$k \equiv$

$$1.380\ 649 \times 10^{-23} \text{ J/K}$$

$e \equiv$

$$1.602\ 176\ 634 \times 10^{-19} \text{ C}$$

From a fixed value of h to a new kg (KIBBLE BALANCE)



From a fixed value of h to a new kg (KIBBLE BALANCE)



Basic principle of KIBBLE BALANCE

electrical force
(electrical current in
magnetic field)
calibrated with
quantum standards

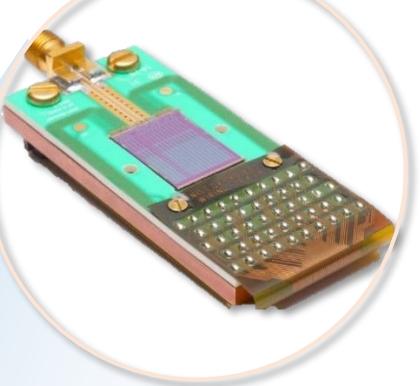
mechanical force
(mass)

Planck constant $h \leftrightarrow$ mass m

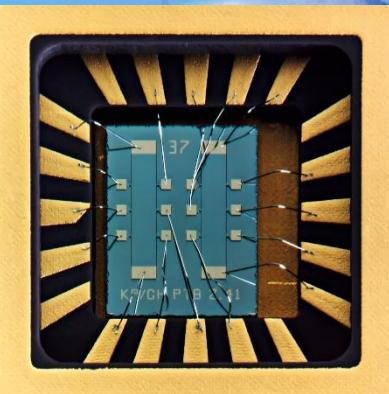
NIST

ELECTRICAL QUANTUM STANDARDS

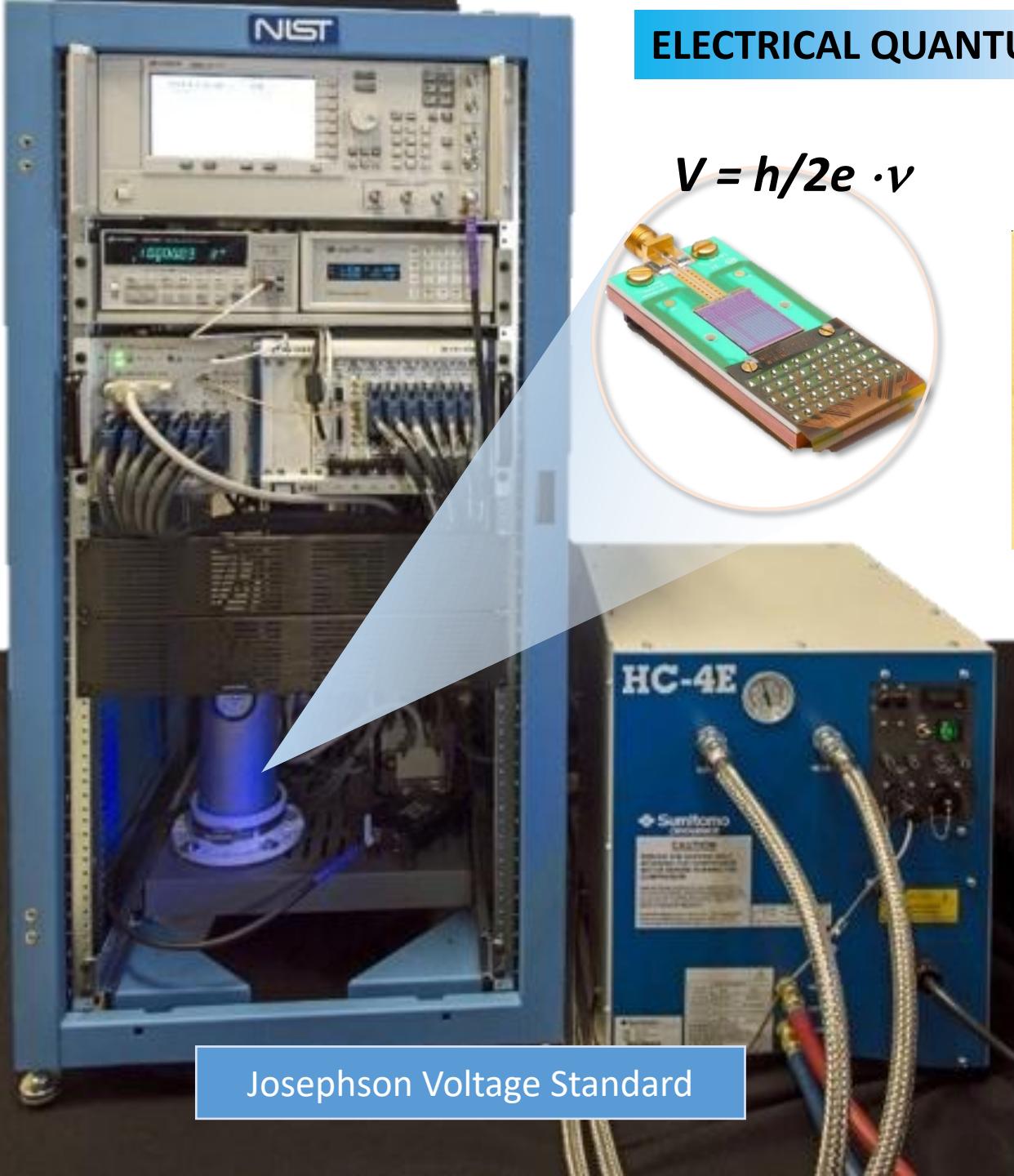
$$V = h/2e \cdot \nu$$



$$R = h/e^2$$



Josephson Voltage Standard



Josephson Voltage Standard

Quantum Hall Resistor



CREDIT: ROBERT RATHE

Industrial Prototype: Planck Balance



Our New SI System



CODATA RECOMMENDED VALUES OF THE FUNDAMENTAL CONSTANTS OF PHYSICS AND CHEMISTRY NIST SP 959 (June 2019)

An extensive constants list is available at physics.nist.gov/constants.

Quantity	Symbol	Numerical value	Unit
* ¹³³ Cs hyperfine transition frequency	$\Delta\nu_{\text{Cs}}$	9 192 631 770	Hz
*speed of light in vacuum	c	299 792 458	m s^{-1}
*Planck constant	\hbar	$6.626\ 070\ 15 \times 10^{-34}$	J Hz^{-1}
	\hbar	$1.054\ 571\ 817\ \dots \times 10^{-34}$	J s
*elementary charge	e	$1.602\ 176\ 634 \times 10^{-19}$	C
*Avogadro constant	N_A	$6.022\ 140\ 76 \times 10^{23}$	mol^{-1}
*Boltzmann constant	k	$1.380\ 649 \times 10^{-23}$	J K^{-1}
*luminous efficacy	K_{cd}	683	lm W^{-1}
electron volt (e/C) J	eV	$1.602\ 176\ 634 \times 10^{-19}$	J
Josephson constant $2e/h$	K_J	$483\ 597.848\ 4\ \dots \times 10^9$	Hz V^{-1}
von Klitzing constant $2\pi\hbar/e^2$	R_K	25 812.807 45...	Ω
molar gas constant $N_A k$	R	8.314 462 618...	$\text{J mol}^{-1} \text{K}^{-1}$
Stefan-Boltzmann const. $\pi^2 k^4/(60\hbar^3 c^2)$	σ	$5.670\ 374\ 419\ \dots \times 10^{-8}$	$\text{W m}^{-2} \text{K}^{-4}$

*Defining constants of the International System of Units (SI).

Calculated von Klitzing constant Corrections to $R_K = h/e^2$?



25812,80745930450666004551670608744304245727322140342176832971607
3228965768572716532282171634884319000217144421378765742752959413401
8357299684093879973315989628069483326708455321978636254281728494658
33207123385987 **QED corrections?** 1950559470887042232733954593703467654
26247139478967514442716119166501055796733958699145001525815707301968
07794523922286571219626039688737836828842906311604825818122439671427
1884015339064744580558045245099408090478648316743222192441638573926
27089910969544523285628937632796 **Gravitational** 6454192845324325022
43547341995061522571701155672571 02649673688649348373
07547633083732603235857721511497 74721314078164034080
8317457760806701512070942690053675429176965840962009638231378317723
8953315269366720535728752400531769855897217630973638284031650531224
50651313357953997757860188836661566148841132888725845344695764980632
61107743566471984685014937992076949684202351009905634780040228805973
410045014483915088251106648700703456225812652449278244365....**Ohm**

Consistency Check of Quantum Standards



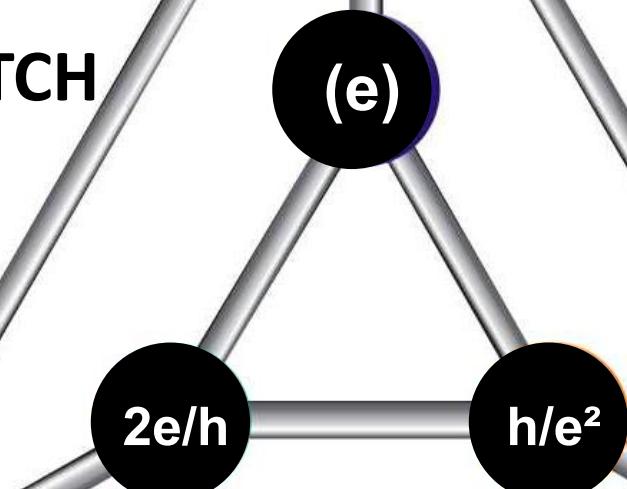
*André-Marie
Ampère*



'civilisational decline'
of Europe ?

A TEST FOR “QUANTUM” IF
VOLTA, OHM, AND AMPERE MATCH

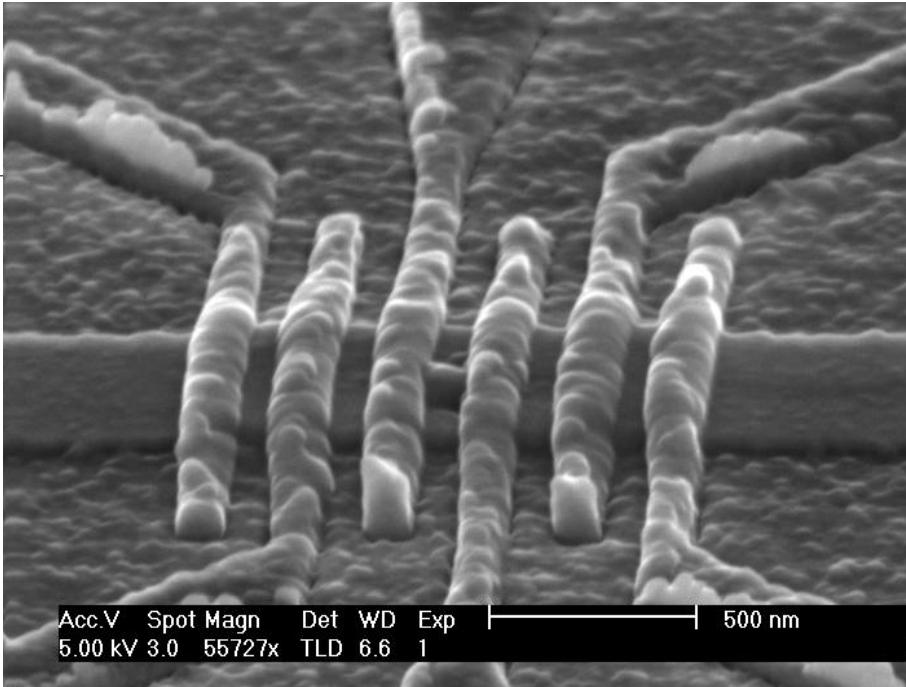
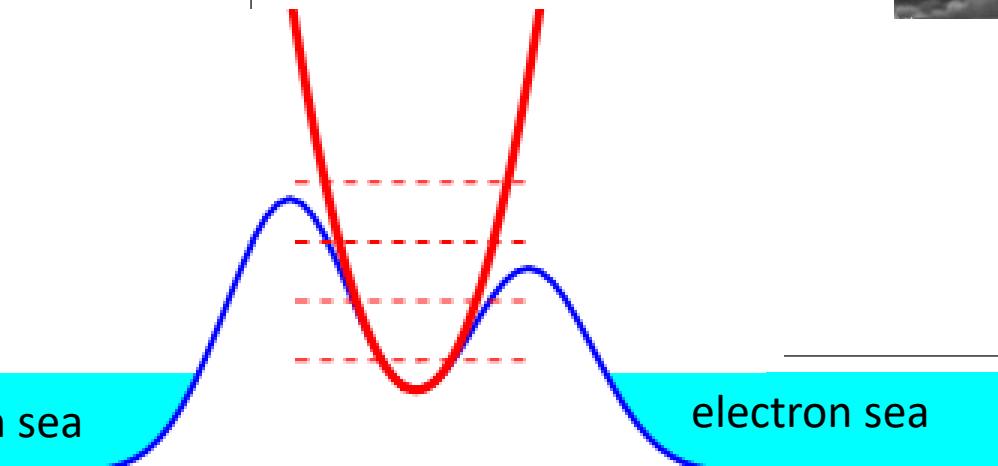
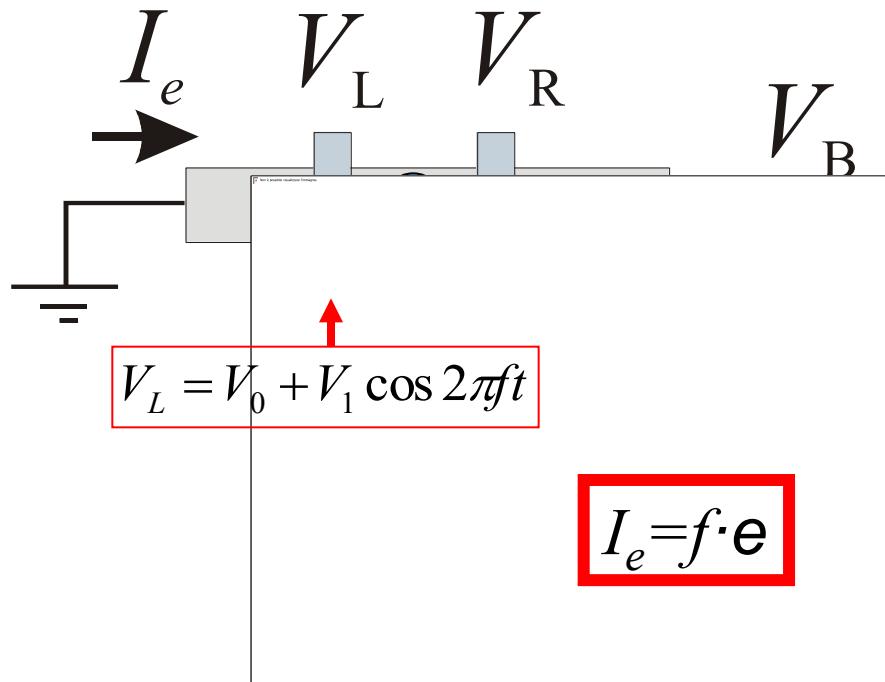
Alessandro Volta



Georg Simon Ohm



Realisation of the ELECTRIC BASE UNIT AMPERE SINGLE ELECTRON PUMP



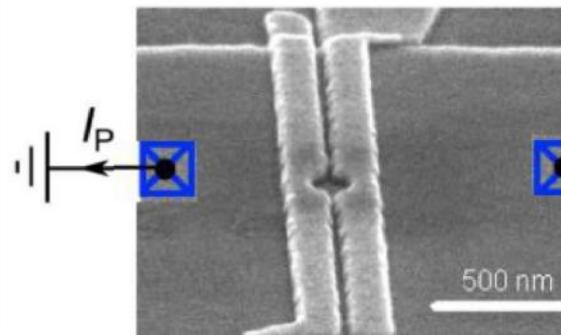
Robust single-parameter
quantized charge pumping
B. Kaestner et. al.
(PTB Braunschweig)

APL 92, 192106 (2008)



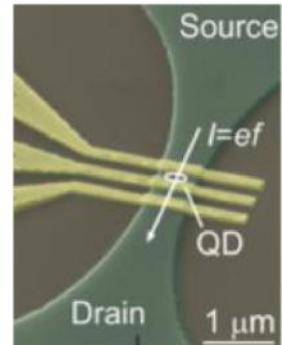
Typical Single Electron Pumps...

(a) GaAs



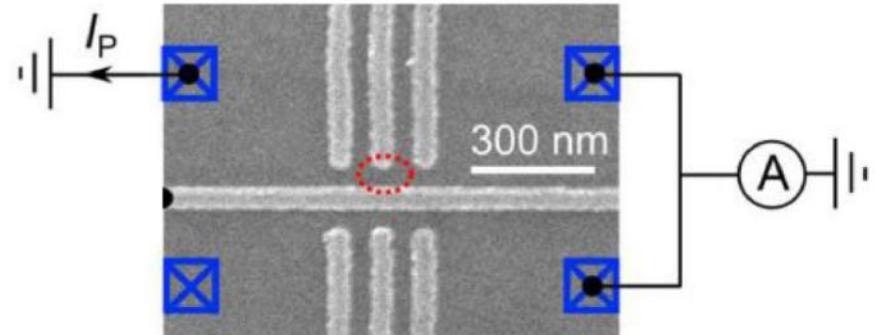
NPL
National Physical Laboratory

(b) GaAs



PIB

(c) GaAs



KRISS
Korea Research Institute of Standards and Science

...with connections to
quantum dot qubits

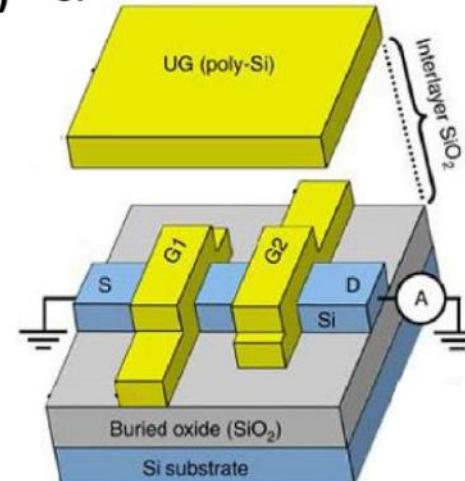
(d)



Si

UNSW
AUSTRALIA

(e)



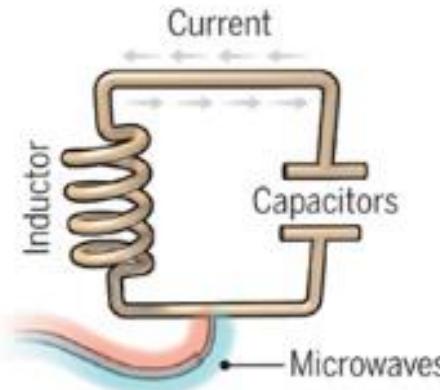
NTT

QUANTUM BITS- the building blocks of quantum computer



A bit of the action

In the race to build a quantum computer, companies are pursuing many types of quantum bits, or qubits, each with its own strengths and weaknesses.

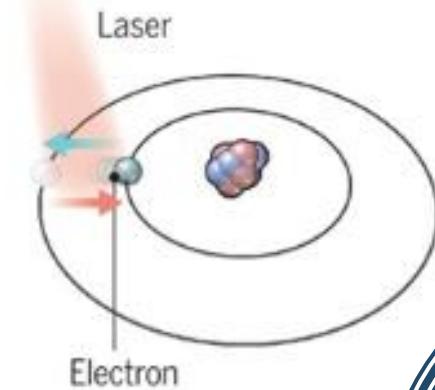


Superconducting loops

A resistance-free current oscillates back and forth around a circuit loop. An injected microwave signal excites the current into superposition states.

Longevity (seconds)

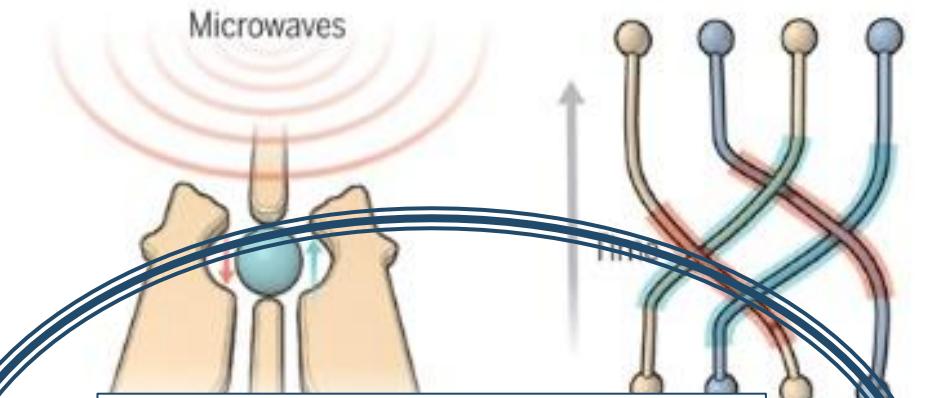
0.00005



Trapped ions

Electrically charged atoms, or ions, have quantum energies that depend on the location of electrons. Tuned lasers cool and trap the ions, and put them in superposition states.

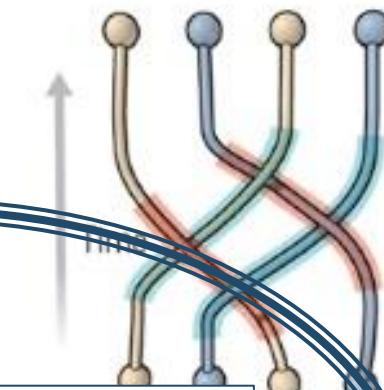
>1000



Silicon quantum dots

These "artificial atoms" are made by adding an electron to a small piece of pure silicon. Microwaves control the electron's quantum state.

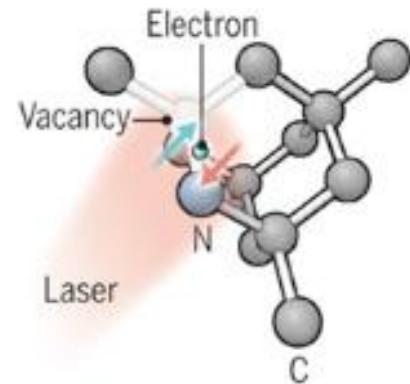
0.03



Topological qubits

Quasiparticles can be seen in the behavior of electrons channelled through semiconductor structures. Their braided paths can encode quantum information.

N/A



Diamond vacancies

A nitrogen atom and a vacancy add an electron to a diamond lattice. Its quantum spin state, along with those of nearby carbon nuclei, can be controlled with light.

10

Logic success rate

99.4%

99.9%

~99%

N/A

99.2%

FERMI and QUANTUM HALL SCIENCE



FERMIIONS:

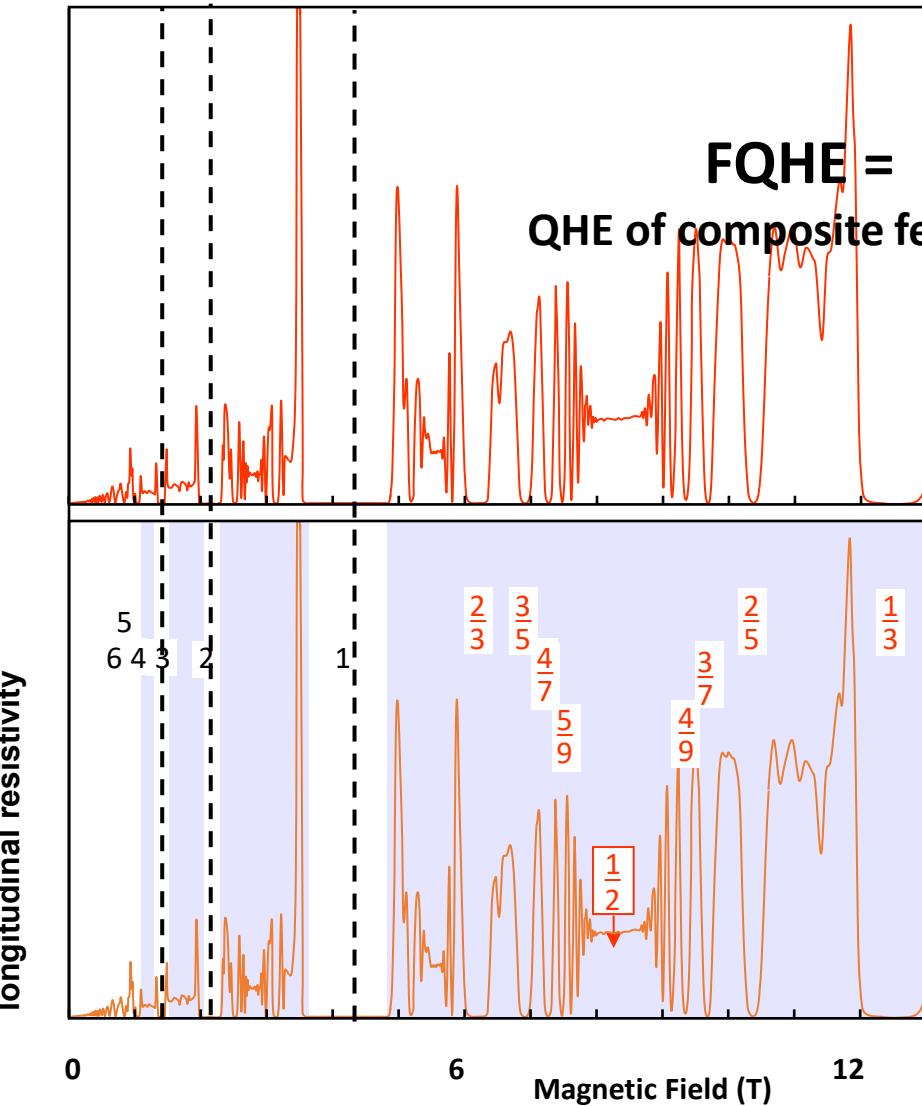
FQHE = QHE of COMPOSITE FERMIONS (*1 electron + 2 flux quanta*)

BOSONS:

QHE = *COMPOSITE BOSONS* (*1 electron + 1 flux quantum*) IN 2-D SYSTEMS

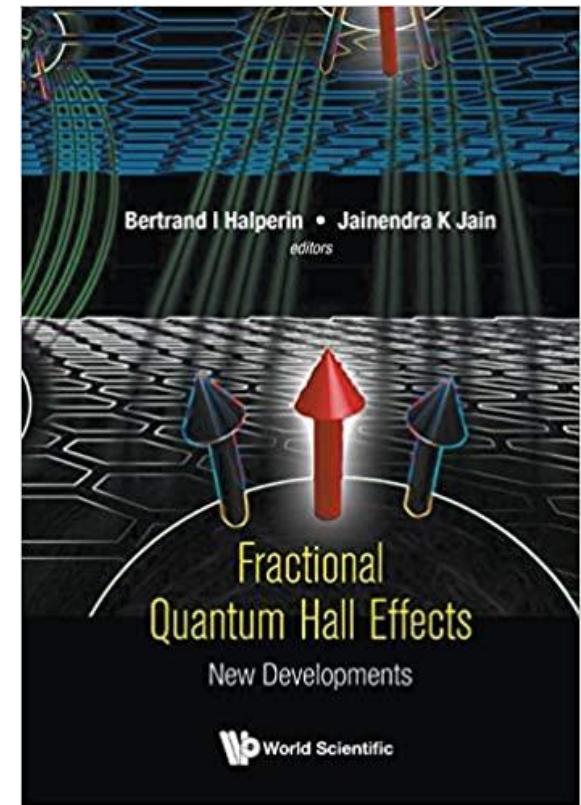
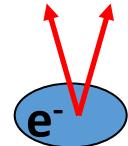
ANYONS: \leftrightarrow Two-dimensional system (2-D SYSTEM)

Quantum Hall Physics

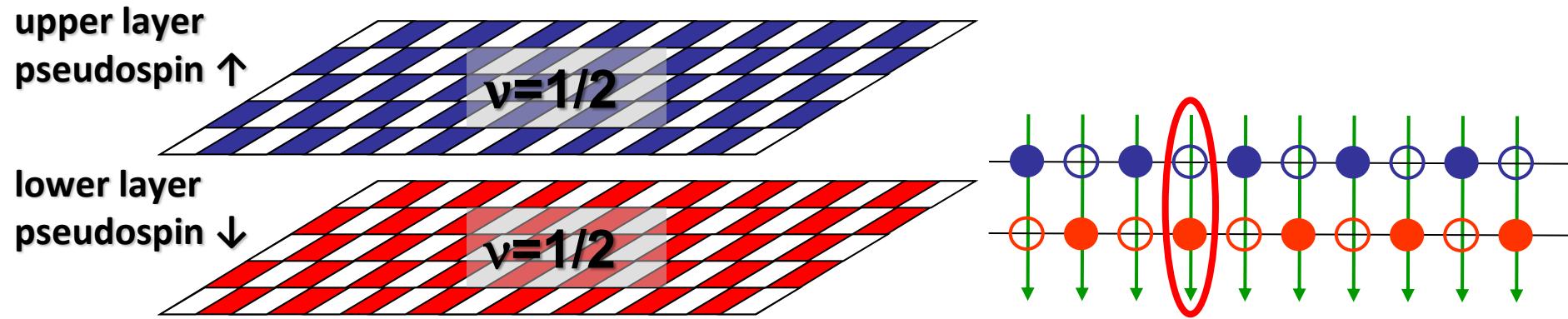


A very powerful quasiparticle
(introduced by Jainandra Jain)

h/e h/e



Bose Condensate of Excitons



Ground State at $n_{\text{tot}}=1$:

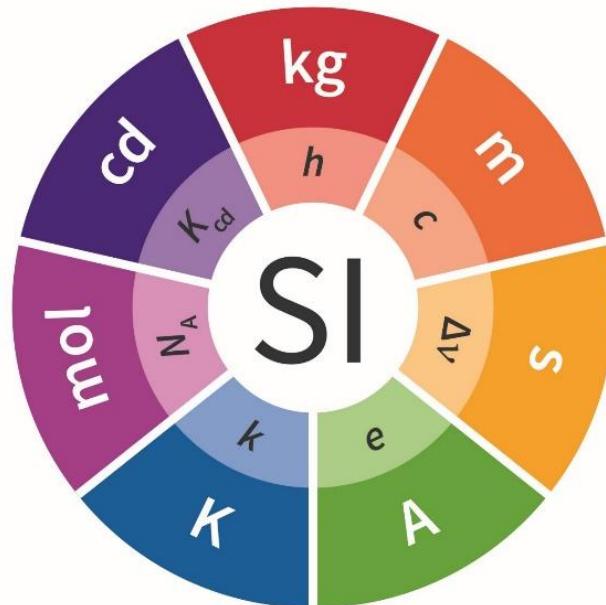
$$|\Psi\rangle = \prod_k (a + b c_{k,\downarrow}^\dagger d_{-k,\uparrow}^\dagger) \left(\prod_k c_{k,\uparrow} |0\rangle \right).$$

Bose-Einstein Condensate of Excitons (with *inter-layer phase coherence*) in the ground state

A Success of Global Cooperation



**The constants of nature are the
most stable basis for a
UNIVERSAL SYSTEM OF UNITS
“*for all times, for all people*”.**



OPEN QUESTION



HOW CONSTANT ARE FUNDAMENTAL CONSTANTS ?

**Sufficiently constant for metrology:
applications**

$$\frac{1}{\alpha} \cdot \frac{\Delta \alpha}{\Delta t} < 10^{-18} \text{ /year}$$

inverse finestructure constant : $\alpha^{-1} = \frac{h}{e^2} \cdot \frac{2}{c \cdot \mu_0}$